Active compression bandage made of electroactive elastomers

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Abstract—Active compression bandages made of electromechanically active elastomers have recently been proposed to counteract dynamically, rather than statically, limb swelling due to various pathologies or conditions. To apply and modulate the compression pressure they exploit the ability of electroactive elastomer layers of changing size in response to a high voltage. For safety reasons such devices must be properly insulated from the user limb. In this work we present an electroactive bandage made of two pre-stretched layers of an electroactive acrylic elastomer sandwiched between two insulating layers of a passive silicone elastomer. Moreover, uniaxial stiffening elements where introduced to maximise actuation along the radial direction. Both experimental investigations and a finite electro-elasticity analytical model showed that the passive layers play a key role for an effective transmission of actuation from the active layers to the load. The prototypes were able to actively vary the applied pressure up to 10%. The model showed that by increasing the number of electroactive layers the pressure variation could be further increased, although with a saturation trend, providing useful indication for future designs of such bandages.

Index Terms— actuator, bandage, compressive, dielectric elastomer, electrical, electroactive, electromechanical, limb, polymer, soft, stretchable.

I. INTRODUCTION

Blood circulation from the lower limbs to the heart depends on vein valves and muscular compression on blood vessels. When those mechanisms are pathological, blood tends to accumulate in the lower limbs [1]. This may cause swelling, pain or lead to even more severe conditions [2], [3]. Treatments for those diseases include both static (passive) and dynamic (active) compression systems, such as stockings and pneumatic sleeves [4], [5]. The former are elastic garments applying a static pressure, typically in the range 20–60 mmHg (2.7–8 kPa) [6], which however have been proved to be less effective than pneumatic systems [7], [8]. On the other hand, the latter require bulky pneumatic cuffs and a pumping box, resulting impractical in many conditions.

An alternative solution to address these issues comes from the use of Dielectric Elastomer (DE) actuators, which were proven to be effective for interacting with soft bodies [9]. In particular, their use for electro-mechanically active bandages was recently proposed [10], [11]. The device was conceived as a stretchable bandage consisting of a single layer of a silicone elastomer with compliant electrodes on both sides. The active bandage was designed to be wrapped around human limbs with an initial maximum pressure that can be dynamically reduced via an applied high-voltage. Considering the high voltage needed to activate the bandage, such device must prevent electrical discharges and guarantee proper insulation from both the human limb and the external environment.

To address this issue, in this work we present a dynamic active bandage featuring silicone elastomer coating layers, acting as insulators. Moreover, the coating layers are analysed also in terms of their effect on the transmission of actuation from the active layers to the load. Furthermore, this paper also presents the following means to improve the performance of such active bandages: a multi-layer structure for the active part, a more-performing active material and a design solution that maximises actuation along the radial direction.

Both experimental tests and a finite electro-elasticity model, specifically developed for the multilayer bandage, were used to investigate the effects on the actuation performance of the number of the active layers and the thickness of the coating passive layers.

II. ACTIVE BANDAGE CONCEPT

The conceived active bandage relies on a particular type of Electromechanically Active Polymers (EAPs), which are smart materials able to respond to applied electrical stimuli with changes of size and/or shape [12], [13]. Specifically, we considered the most performing EAP technology, known as Dielectric Elastomer (DE) actuators [14]–[17].

DE actuators are electromechanical transducers essentially made of a thin layer of an insulting elastomer coated on both sides with compliant electrodes. When a voltage \( V \) is applied between the electrodes of a planar DE actuator, the following effective electrostatic pressure \( p \), parallel to the electric field \( E \), is generated [14]:
\[ p = \varepsilon_0 \varepsilon_r (V/d)^2 = \varepsilon_0 \varepsilon_r E^2, \]  

where \( \varepsilon_0 \) is the dielectric permittivity of vacuum, \( \varepsilon_r \) is the relative dielectric constant of the elastomer and \( d \) is the thickness of the dielectric layer. This pressure squeezes the soft dielectric layer causing a reduction of its thickness and a concomitant expansion of its area [14].

The bandage was conceived as a thin, stretchable and electro-responsive multilayer structure of elastomer films, to be wrapped around limbs (Fig. 1). Two active layers \((a_1 \text{ and } a_2)\) are sandwiched between two passive layers \((p_1 \text{ and } p_2)\). Wooden stiffeners are embedded within the outer passive layer longitudinally in order to maximise actuation radially. Velcro stripes allow for securing the bandage to the limb.

Each inner active layer consists of a DE film coated with compliant electrodes. The two active layers are then coupled to thicker and softer passive layers. The passive layers have two key functions. Firstly, they serve as a mechanical interface with the limb, aimed at reducing the constraining effect introduced by the latter on the electrically induced deformation of the active layers. Secondly, as the proposed prototype bandage requires high driving voltages (as detailed in the following), the passive layers also ensure electrical safety, providing insulation.

Wooden stiffening sticks were embedded within the outer passive layer, with the aim of maximising actuation (variation of pressure) along the radial direction, preventing elongations of the bandage longitudinally. Indeed, combining a DE actuator with unstretchable elements has previously been demonstrated to be effective for unidirectional actuation [18].

The bandage was conceived to be wrapped around the limb with a certain prestretch, thus applying a certain passive pressure. When a voltage \( V \) is applied between the electrodes, the bandage is able to partially release the initial passive pressure, by increasing its circumference. Therefore, by modulating the applied voltage it is possible to continuously vary the applied pressure.

As mentioned above, prior to this work other investigators have reported on the use of DE actuators to develop active bandages [10], [11]. The peculiarities of the approach described here are: 1) two active layers were stacked together to increase the strength of the system; 2) the active layers were made of an acrylic elastomer film showing one of the highest electromechanical transduction performance, in terms of maximum achievable strains and stresses; 3) stiffening sticks were used to maximise actuation along the radial direction; 4) two thick and soft passive layers were used as interfaces with suitable properties in terms of mechanical compliance and electrical safety. The effects of these improvements were investigated theoretically and experimentally as reported in the following sections.

III. ACTIVE BANDAGE SPECIFICATIONS

The bandage should be able to apply a maximum pressure comparable to those of elastic compression stockings, i.e. 1-6 kPa [19], and then reduce the pressure upon electric driving. The literature does not offer any widely accepted exact estimate on the variation of pressure required to compensate for a deficient blood return. This is likely due to the variability of individual pathological and anatomical conditions. Indeed, for any given deficit, the compensation pressure could vary significantly according to the size of the limb, especially due to the thickness of muscles and adipose tissue. So, instead of targeting a specific performance, this work was aimed at validating the functionality of the proposed concept. This was achieved by manufacturing and characterising prototypes, as described below.

IV. MANUFACTURING OF PROTOTYPE ACTIVE BANDAGES

Proof-of-concept prototype bandages were manufactured as follows. The active layers consisted of an acrylic elastomer film (VHB 4910, 3M, USA). This material was chosen in consideration of its well-known high electromechanical transduction performance in terms of achievable active stress [14], [15] and its adhesive properties, which simplified the manufacturing process by ensuring proper bonding between layers. The compliant electrode material consisted of carbon black powder (Vulcan XC72, Cabot Corporation, USA). The passive elastomeric layers were made of a soft silicone elastomer (TC-5005 A/B-C, BJB Enterprises Inc., USA), which was used with a content of softening agent C equal to 50 wt%. The passive elastomeric layers were produced by mould casting as films of different thickness, ranging from 2 to 4 mm. The different films were used to manufacture different samples of the bandage, in order to investigate how the electromechanical performance was affected by the thickness of the passive layers. Six wooden stiffening sticks, having a diameter of 2.5 mm each, were integrated within the outer passive layer, during its fabrication by mould casting, according to the layout shown in Fig. 2.

Electrical contacts for the electrodes were obtained by means of metal stripes integrated within the structure. Velcro stripes were glued at the two ends of the bandage, so as to secure it to the limb (Fig. 2).

The overall manufacturing process consisted of the following steps. A single active layer with a thickness at rest of 2 mm was obtained by coupling together two unstretched 1 mm-thick VHB 4910 films. This was justified by preliminary experimental evidences, which had shown superior force generation capabilities from actuators featuring thicker active layers. The resulting film was then equi-biaxially prestretched.
by 300% and attached to a support frame. The use of that pre-strain was justified by its well-known beneficial effect in terms of electromechanical performance increase, as first reported by [14] and then explained in different ways by [16] and [20]. The prestretch caused a reduction of the thickness from 2 to 0.125 mm.

Fig. 2. Schematic drawing (top) and picture (bottom) of a prototype active bandage.

A first compliant electrode (250 mm × 120 mm) was then created by depositing an alcohol-based suspension of the carbon black powder on one of the surfaces of the active layer. Then, a metal stripe connector was attached to it. A second active layer was coupled to the first one, covering the electroded side. The outer surfaces of the two-layer structure were coated with the carbon black powder to obtain analogous compliant electrodes and were fitted with metal stripe connectors.

In order to create the passive layers, the active layer sandwich was laid at the bottom of a mould and then coated with the silicone material in liquid form, which was poured into the mould. The mould was maintained horizontally for curing at room temperature for 24 hours. After curing, the obtained multi-layer structure was removed from the mould and flipped over, and the same procedure was repeated in order to cast the second passive layer. During this process, six wooden sticks were also integrated on one side of the structure, by placing them on the surface of the active layer before the deposition of the silicone. The sticks allowed for holding the pre-stretch along one direction upon the removal of the bandage from the supporting frame.

The resulting self-standing bandage acquired the shape visible in Fig. 2. The extent of inevitable shrinking between two adjacent sticks depended on the passive layers thickness, according to the mechanical resistance offered by the passive coatings. Owing to that reason, it was not possible to obtain self-standing bandages with a passive layer thickness lower than 2 mm.

V. TESTING OF THE PROTOTYPE ACTIVE BANDAGES

In order to test the performance of the different prototype bandages, a chamber that mimicked the compliance of a human limb was assembled. It consisted of a soft tubular structure containing pressurized air, as shown in Fig. 3a. It was constructed by coupling together two soft rubber membranes (model 4075 triaxial test rubber membrane, Wykehman Farrance, UK), having each a diameter of 70 mm and a thickness of 0.4 mm, and combining them with two rigid sealing plugs. The sealing plugs were connected one another by a rigid spacer, setting to 180 mm the distance between the two inner plugs edges. A manual pump, connected to one of the sealing plugs, allowed for pressurizing the air chamber. Pressure readings were taken from a digital pressure gauge (model Bit02B-2.5 bar, AEP Transducers, Italy), connected to the other sealing plug (Fig. 3).

Fig. 3. Testing of the prototype dynamic bandages: air chamber that mimicked the compliance of a human limb, without (a) and with (b) the bandage.

The bandage was secured (by means of the Velcro stripes) to the air chamber, such that the stiffening sticks were oriented axially (Fig. 3b). The chamber pressure was initially set to \( P_0 = 7.5 \) kPa for each prototype bandage tested. Therefore, the different bandages reached different initial values of their diameter, according to the different values of their passive layer thickness (and, so, their stiffness).

From this initial state, increasing voltages were applied, with steps of 500 V, until electrical breakdown of the bandage occurred. As a result of the radial actuation, the internal chamber pressure \( P_V \) reached a lower value, monitored with the pressure gauge. Results of the testing of three samples of the bandage with a passive layer thickness \( D_p \) of 2, 3 and 4 mm are presented in Fig. 4. The data show that 3 mm was an ‘optimum’ value, among those tested, for the passive layer thickness.
In order to obtain an analytical description of the system, an axisymmetric model of the bandage based on finite electro-elasticity was developed as described below.

**VI. ANALYTICAL MODEL OF THE ACTIVE BANDAGE**

The model neglected the viscoelastic behaviour of each layer and described its nonlinear electromechanical properties using a Neo-Hookean hyper-electro-elastic representation.

The model was developed for a central portion of the tubular structure, which was assumed to be sufficiently distant from the two ends of the tube to neglect any variation of pressure along the longitudinal coordinate $z$. Moreover, in consideration of the fact that the stiffening sticks constrain the longitudinal stretch to a fixed value, the length along the $z$-axis was considered constant (140 mm, see Fig. 2). Therefore, the problem was studied assuming a plane strain condition, implying a longitudinal stretch $\lambda_z = 1$ for the passive layers and $\lambda_z = 4$ for the active ones.

### A. Kinematics of the multilayer structure

To describe the geometry of the system, the three deformed configurations reported in Fig. 5 were considered.

In the “initial state” $B_h$ (Fig. 5 top), the bandage is wrapped around the air chamber with a circumferential length at the interface of 260 mm. Here, the system is in equilibrium with an air chamber pressure $P_{c0}$ and a contact pressure between the bandage and the chamber’s rubber membrane $P_{cb}$. It is worth pointing out that when the bandage is applied to the chamber and the latter is pressurized, the azimuthal or hoop stress is distributed between the rubber membrane and the bandage, according to their stiffness. In this state $B_h$, which is reached when the planar bandage is bent to reach the cylindrical configuration, the length of the inner circumference of the passive layer $p_1$ was assumed to be equal to the length (260 mm) of the unbent bandage (Fig. 2). This way, the inner boundary of the layer $p_1$ has a hoop stretch $\lambda_{1b}=1$. In principle, it should be considered that, while bending the multilayer, a non-homogeneous deformation is imposed [21], which would induce a radius-dependent hoop stretch in the layers. However, due to the thinness of the strata, only the stretch of the midline of each layer $\lambda_{b,lay}$ (where ‘lay’ indicates the layer, namely $\text{lay}=m$, $p_1$, $a_1$, $a_2$, $p_2$) was considered in our model. A straightforward computation shows that for the active layers $a_1$, $a_2$ this hoop stretch ranges between 4.196 and 4.388 (as these layers are initially prestretched with a factor 4), while $\lambda_{b,p_1}$ ($\lambda_{b,p_2}$) ranges between 1.024 (1.075) and 1.046 (1.140). The stretch $\lambda_{b,m}$ is assumed unitary. Table 1 reports the calculated hoop stretches.

<table>
<thead>
<tr>
<th>$D_p$ (mm)</th>
<th>$\lambda_{b,p_1}$</th>
<th>$\lambda_{b,a_1}$</th>
<th>$\lambda_{b,a_2}$</th>
<th>$\lambda_{b,p_2}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>1.024</td>
<td>4.196</td>
<td>4.208</td>
<td>1.075</td>
</tr>
<tr>
<td>3</td>
<td>1.035</td>
<td>4.284</td>
<td>4.296</td>
<td>1.108</td>
</tr>
<tr>
<td>4</td>
<td>1.046</td>
<td>4.376</td>
<td>4.388</td>
<td>1.140</td>
</tr>
</tbody>
</table>

In the “Voltage OFF” state $B_e$ (Fig. 5 centre), the bandage is secured to the air chamber with a certain circumferential stretch, assigned when the air chamber pressure $P_{c0}>P_{b0}$ is set to 7.5 kPa. In this state, the contact pressure between the rubber membrane and the active bandage is $P_{e0}>P_{cb}$. In the “Voltage ON” state $B_v$ (Fig. 5 bottom), a voltage $V$ generates a radial expansion of the bandage, which behaves like a cylindrical DE actuator [22], [23]. The radial expansion causes an active reduction of both the chamber’s internal pressure and the contact pressure applied to the chamber, respectively from $P_0$ to $P_{v}<P_0$ and from $P_{e0}$ to $P_{v}<P_{e0}$. In this state, the hoop stretch in the generic layer $\lambda_{b,lay}(r)$ is given by:

$$\lambda_{b,lay}(r) = \frac{r}{R} \lambda_{b,lay} = \frac{r}{\sqrt{R_{in,lay}^{2} + \lambda_{lay}^{2} (r_{2}^{2} - r_{1}^{2})^{2}}} \lambda_{b,lay}, \quad (2)$$

where $\text{lay}=m$, $p_1$, $a_1$, $a_2$, $p_2$ and $R_{in,lay}$ denotes the inner radius of layer ‘lay’ in state $B_h$. In (2), the ratio $r/R$ is the hoop stretch with respect to $B_h$, while $\lambda_{b,lay}$ takes into account the deformation undergone by the multilayer in state $B_h$. The square root term is an alternative expression for the radius $R$, obtained by taking into account the constraint of incompressibility of the elastomeric material, i.e. $\lambda_r \lambda_z \lambda_{a} = 1$, which is useful to compute the radial stretch $\lambda_r$, recalling that $\lambda_z = 1$.

### B. Electro-mechanics of a single layer

In order to describe the overall behaviour of the multilayer, it is useful to recall the governing equations for a single layer in a cylindrical reference system.

Let us assume that the current inner and outer radii of an DE cylindrical actuator are $r_i$ and $r_e$, respectively, and that at the two cylindrical surfaces the radial tensile stresses $\sigma_r(r_i)$ and $\sigma_r(r_e)$ are applied. In addition, the surfaces are coated with perfectly stretchable electrodes subjected to a voltage $V$, which induces through the thickness a radial electric field $E(r)=E_r(r)$.

An application of the Gauss’ theorem at a generic radial distance within the dielectric provides a relation between $E$ and the amount of charge $Q$ stored on one electrode:

$$\int_{r_i}^{r_e} E \, dr = \frac{Q}{\pi R^2}.$$
where \( \varepsilon = \varepsilon_0 \varepsilon_r \) is the absolute dielectric permittivity of the elastomer.

By integrating (3) with respect to the radius while considering the well-known relation between the electric potential \( \varphi \) and electric field \( E \) for a cylindrical capacitor having an axial length \( L \), we obtain the relation between \( Q \) and the applied voltage \( V \):

\[
V = \varphi(r_i) - \varphi(r_e) = \int_{r_i}^{r_e} -d\varphi = \int_{r_i}^{r_e} Edr = \frac{Q}{2\pi \varepsilon_0 \varepsilon_r L} \int_{r_i}^{r_e} \frac{1}{r} dr = \frac{Q}{2\pi \varepsilon_0 \varepsilon_r L} \ln \frac{r_e}{r_i},
\]

so that

\[
E = \frac{1}{r} V/\ln \frac{r_e}{r_i}.
\]

The layer, incompressible, obeys an isotropic hyper-electro-elastic strain energy \( W(\lambda_r, \lambda_\theta, \lambda_z, E) \). In this configuration, the constitutive equations can be written as (see Appendix):

\[
D = -\frac{\partial W}{\partial E},
\]

\[
\sigma_\theta - \sigma_r = \lambda_\theta \frac{\partial W}{\partial \lambda_\theta} - \lambda_r \frac{\partial W}{\partial \lambda_r} - DE,
\]

\[
\sigma_z - \sigma_r = \lambda_z \frac{\partial W}{\partial \lambda_z} - \lambda_r \frac{\partial W}{\partial \lambda_r} - DE,
\]

where \( D \) is the electric displacement, which has only a radial component, according to (6).

Under the action of an axisymmetric electromechanical loading, the equilibrium of each layer is governed, in terms of Cauchy total stress \( \sigma \), by the following differential equation:

\[
d\sigma_r + \frac{\sigma_r - \sigma_\theta}{r} = 0.
\]

Integration of (9) between \( r_i \) and \( r_e \) provides

\[
\sigma_r(r_e) - \sigma_r(r_i) = \int_{r_i}^{r_e} \frac{\sigma_\theta - \sigma_r}{r} dr.
\]

In our model, an extended neo-Hookean strain energy function was adopted to compare model predictions with experimental results. Its general expression is

\[
W = \frac{1}{2} \mu (\lambda_r^2 + \lambda_\theta^2 + \lambda_z^2 - 3) - \frac{\varepsilon}{2} (E_k E_k)^2,
\]

where \( \mu \) is the initial shear modulus, the index \( k = r, \theta, z \) and where the Einstein summation convention is adopted. The incompressibility of the elastomer requires that \( \mu = Y/3 \), where \( Y \) is its Young’s modulus. Therefore, the in plane constitutive equations for the layer specialise to

\[
\sigma_\theta - \sigma_r = \lambda_\theta \frac{\partial W}{\partial \lambda_\theta} - \lambda_r \frac{\partial W}{\partial \lambda_r} - DE = \varepsilon E,
\]
where it is clearly seen that (11) admits the classical linear relationship (12) among electric displacement and electric field.

Eq. (8) can be employed to find $\sigma_z$ at each point once $\sigma_r$ has been computed.

In addition, the pressure difference $\sigma_r(r_e) - \sigma_r(r_i)$ becomes

$$\sigma_r(r_e) - \sigma_r(r_i) = \int_{r_i}^{r_e} \frac{\mu (\lambda_0 - \lambda_0^2 \lambda_z^2)}{r} \left( \frac{1}{r \ln \frac{r'}{r_i}} \right)^2 dr.$$  \hspace{1cm} (14)

It is worth pointing out that, while a closed form of the integral in (14) can be obtained, this will not be given here.

C. Voltage-pressure relationship for the multilayer bandage

The voltage pressure relationship for the bandage in state $B_V$ can be obtained by imposing continuity of the radial stresses at the interface between two generic concentric layers and the following boundary conditions:

$$\sigma_r(r_m) = -P_v, \quad \sigma_r(r_{p2}) = 0.$$ \hspace{1cm} (15)

A repeated use of (14), where $V=0$ in layers $m$, $p_1$ and $p_2$, yields

$$P_v = \int_{r_m}^{r_{p1}} \frac{\mu_{m}}{r} (\lambda_{0m}^2 - \lambda_{0m}^2 \lambda_{zm}^2) dr + \int_{r_{p1}}^{r_{a1}} \frac{\mu_{p1}}{r} (\lambda_{0p1}^2 - \lambda_{0p1}^2 \lambda_{zp1}^2) dr + \int_{r_{a1}}^{r_{a1a2}} \frac{\mu_{a1}}{r} (\lambda_{0a1}^2 - \lambda_{0a1}^2 \lambda_{za1}^2) - \epsilon \left( \frac{1}{r \ln \frac{r}{r_{a1}}} \right)^2 dr + \int_{r_{a1a2}}^{r_{a2}} \frac{\mu_{a2}}{r} (\lambda_{0a2}^2 - \lambda_{0a2}^2 \lambda_{za2}^2) - \epsilon \left( \frac{1}{r \ln \frac{r}{r_{a1a2}}} \right)^2 dr + \int_{r_{a2}}^{r_{p2}} \frac{\mu_{p2}}{r} (\lambda_{0p2}^2 - \lambda_{0p2}^2 \lambda_{zp2}^2) dr.$$ \hspace{1cm} (16)

Assuming that the product between the pressure $P_v$ and the air volume $Vol$ inside the chamber only depends on the mechanical path (i.e. assuming that the temperature is constant) and assuming no air leakage from the chamber, the ideal gas law gives

$$P_v Vol = \text{constant}.$$ \hspace{1cm} (17)

This condition allows for relating the inner radius of the rubber membrane $r_m$ to the pressure $P_v$:

$$P_0 r_m^2 = P_v r_m^2.$$ \hspace{1cm} (18)

By substituting (18) into (16), a relation between the air chamber pressure $P_0$ and the inner radius of the rubber membrane $r_m$ is provided, once the driving voltage $V$ is assigned:

$$\int_{r_m}^{r_{p1}} \frac{P_m}{P_0} \left( \lambda_{0m}^2 - \lambda_{0m}^2 \lambda_{zm}^2 \right) dr + \int_{r_{p1}}^{r_{a1}} \frac{P_m}{P_0} \left( \lambda_{0p1}^2 - \lambda_{0p1}^2 \lambda_{zp1}^2 \right) dr + \int_{r_{a1}}^{r_{a1a2}} \frac{P_m}{P_0} \left( \lambda_{0a1}^2 - \lambda_{0a1}^2 \lambda_{za1}^2 \right) - \epsilon \left( \frac{1}{r \ln \frac{r}{r_{a1}}} \right)^2 dr + \int_{r_{a1a2}}^{r_{a2}} \frac{P_m}{P_0} \left( \lambda_{0a2}^2 - \lambda_{0a2}^2 \lambda_{za2}^2 \right) - \epsilon \left( \frac{1}{r \ln \frac{r}{r_{a1a2}}} \right)^2 dr + \int_{r_{a2}}^{r_{p2}} \frac{P_m}{P_0} \left( \lambda_{0p2}^2 - \lambda_{0p2}^2 \lambda_{zp2}^2 \right) dr.$$ \hspace{1cm} (19)

In order to calculate the contact pressure $P_c$ it is important to define the pressure sustained by the rubber membrane of the air chamber $P_m$. Considering equation (19), for a certain value of the radius $r_m$ the pressure $P_m$ is given by the first term on the right-hand side of (16):

$$P_m = \int_{r_m}^{r_{p1}} \frac{\mu_{m}}{r} (\lambda_{0m}^2 - \lambda_{0m}^2 \lambda_{zm}^2) dr.$$ \hspace{1cm} (20)

In the state $B_V$, the contact pressure between the rubber membrane and the bandage is obtained by subtracting $P_m$ from the air chamber pressure $P_V$:

$$P_c = P_V - P_m.$$ \hspace{1cm} (21)

In order to quantify the contact pressure $P_c$ it is necessary to know the shear moduli of the three materials (silicone, acrylic and rubber). For the passive layers, the quasi-static value 16 kPa experimentally determined by [24] was adopted for both the moduli $\mu_{p1}$ and $\mu_{p2}$. For the acrylic elastomer, the value 73 kPa measured by [25] was used for both the moduli $\mu_{a1}$ and $\mu_{a2}$. For the rubber membrane, the value 666 kPa reported in [26] was employed for the modulus $\mu_{m}$.

VII. Model Validation: Comparison Between Experimental Data and Model Predictions

As a validation of the model, Fig. 6 presents a comparison between experimental data and model predictions.

The comparison shows that the model accuracy increases with the thickness of the passive layer. This outcome may be explained in terms of the constraining effect introduced by the stiffening sticks. Indeed, for the sample with 2 mm-thick passive layers the wooden sticks were closer to the electroactive layer, inducing local stress concentration and, so, limiting actuation. As in the model the presence of the stiffeners was ignored, these effects were not considered.

This might explain the discrepancy evident in Fig. 6a, especially at high voltages. Conversely, for the other extreme
case, i.e. for the 4 mm-thick passive layers, the stiffening sticks were significantly distant from the electroactive layer, such that stress concentration and expansion restraining were significantly reduced. This might justify the accurate match between experimental measurements and model predictions evident from Fig. 6c.

VIII. Model Predictions: Contact Pressure

The validated theoretical framework described above is particularly useful to compute the contact pressure \( P_c \) exchanged between the air chamber and the bandage in the ‘Voltage ON’ state. This is an important variable as, with reference to the intended application, it represents the pressure that would actually be exerted by the bandage on the surface of the user. Fig. 7 presents the estimates for the three prototype bandages, while Fig. 8 compares the contact pressure variation \( \Delta P_c \) as a function of the applied voltage \( V \) for bandages having a passive layer’s thickness from 0 to 4 mm and a length of the inner circumference of the passive layer \( p_1 \) equal to \( L=260 \) mm.

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Fig. 6. Dependence of the air chamber pressure \( P_p \) on the applied voltage \( V \): comparison between experimental data and model-based predictions, for the three types of prototype bandages having different thickness \( D_p \) of their passive layers.

Fig. 7. Dependence of the contact pressure \( P_c \) on the applied voltage \( V \) for the three types of prototype bandages having different thickness \( D_p \) of their passive layers.

Fig. 8. Variation of the contact pressure between the air chamber and the bandage, as estimated from the model for bandages having a different thickness \( D_p \) of the passive layers.

Fig. 7 shows the contact pressure-voltage curves for the three prototypes. The curves intersect close to the experimental breakdown limit. For \( D_p=2, 3 \) and 4 mm the estimated initial contact pressure was 6.78, 6.67 and 6.57 kPa, respectively, and upon actuation at 8 kV the pressure respectively dropped to 6.09, 6.06 and 6.03 kPa, corresponding to a reduction of 10.2%, 9.15% and 8.2%. These estimates indicate that the contact pressure change was highest for the sample featuring the thinnest passive layers.

The fact that the model predicts a higher performance for a lower thickness of the passive layers is also evident from Fig. 8, which plots the pressure variation also for values of thickness not tested experimentally.

So, according to the model, the highest performance would be achieved without any passive layer. This outcome is due to the fact that the presence of the stiffeners was neglected by the simplified model. Therefore, further developments of the
model are needed in order to take in account the effect of the stiffeners. By taking into account the stiffeners, it is reasonable to expect an optimum value of the passive layer thickness, which should maximise the contact pressure variation.

IX. FUTURE DEVELOPMENTS

A. Improvement of the electromechanical properties

In order to study the influence of the number of electroactive layers on the actuator’s ability to vary the contact pressure, the simulations shown in Fig. 9 were performed. They refer to bandages having \( D_p = 2 \) mm and an increasing number of active layers with properties identical to those considered above. The simulations show that the higher the number of active layers, the larger is the contact pressure variation, although it tends to saturate.

This outcome is plausible as it is consistent with the intuitive view that, as the total number of layers increases, any constraint at the surfaces of the cylindrical stack tends to have a vanishing influence on the ‘central’ layers that are ‘sufficiently distant’ from the ends. Moreover, as the total number of layers increases, the number of the ‘central’ layers unaffected by the constraint increases, such that the unaffected portion of stack is larger. So, as the stack grows up, it gets closer to an ideal infinitely thick structure, whose generated force is not affected by any constraint at the two ends and by the number of layers: it would generate the same force as that generated by a single ideal unloaded layer. Knowing that such a saturation effect exists is useful for the design of multilayered electroactive bandages.

B. Improvement of the model

To improve the accuracy of the model, the presence of the stiffening sticks should be taken into account. Such a detailed modelling was beyond the aims of this first investigation and should be tackled in future studies.

C. High-voltage driving: viability and challenges

These prototype bandages required driving voltages of several kilovolts. In terms of electrical safety, dealing with such high voltages is clearly not desirable. However, this drawback is mitigated not only by the use of insulating layers, but, especially, by the fact that there’s no need for a high driving current (and, so, power). Indeed, electrically the bandage is a capacitive load, which allows for using low-power, electrically safe sources.

The low power requirement favours also the technical viability of high voltage driving. Indeed, high-voltage multipliers with low-power and compact size (volume of the order of 1 cm\(^3\) or less) are commercially available such as those produced by EMCO High Voltage [27]. This allows for implementations of battery-powered portable and compact systems.

Nevertheless, the need for high-voltage circuitry introduces a significant limitation in terms of costs. This drawback, which is characteristic for the whole field of the DE transducers today, is focusing efforts to produce films that can be driven at lower voltages. Besides fundamental attempts to synthesize new elastomers with higher dielectric constant [28], [29], the most readily achievable solution in the short term is represented by thin-film processing of conventional materials [17]. Indeed, several groups have already demonstrated DE transducers with voltages reduced to a few hundred volts [30], thus anticipating that in the near future the DE technology will likely adopt the standard and cheaper circuitry used today for piezoelectric drives.

X. CONCLUSIONS

We presented here a multilayer active bandage made of dielectric elastomer actuators. This study showed the following main evidences.

First, the passive layers coating the bandage have a function that goes beyond those of electrical protection and mechanical impedance matching. Indeed, as shown by both the experiments and analytical model, they play a key role for an
effective transmission of actuation from the active layers to the load.

The second evidence is that by adopting the multilayer design reported above and different constitutive materials, it was possible to achieve a higher contact pressure drop as compared to previous studies. Indeed, the best performing active bandage prototype reported in [10] allowed for achieving an initial contact pressure of 2.87 kPa and a drop to 2.73 kPa, corresponding to a 5.2% decrease, for a voltage of 11.3 kV; in comparison, the active bandage prototypes presented here allowed for contact pressures ranging from 6.57 kPa to  6.78 kPa and, respectively, pressure drops from 8.2% to 10.2%, for a voltage of 8.5 kV.

The third evidence is that, according to the new design, the existence of an optimum value of the passive layer thickness is expected. However, such value could not be precisely identified here, owing to the need for advanced models able to capture the complexity of the constraints introduced by the stiffening elements.

The fourth evidence is that, for a given passive layer’s thickness, the variation of contact pressure increases with the number of active layers, with a saturation trend.

These outcomes, together with the theoretical framework specifically developed for the case of prestretched multiple layers, are expected to serve as help for future improvements of the design, implementation and manufacturing process of prestretched multi-layer electroactive bandages.

**APPENDIX**

The general constitutive equations for an electroactive, incompressible, isotropic dielectric elastomer expressed in terms of principal stretches $\lambda_i$, electric field $E_i$ and electric displacement field $D_i$ ($i=1,2,3$) are obtained below. In the following, in order to maintain the Einstein convention implying summation over an index repeated twice, for generic quantities $A_i$ and $B_i$ ($i=1,2,3$) it is useful to introduce the notations $[A B]_i$ and $[A B]$, which correspond to $A_i B_i$ and $A_i B_i$, respectively.

Due to the large strains accompanying the deformation of DE materials, constitutive equations are usually defined in terms of nominal quantities, such as principal components of nominal total stress $S_i$, nominal electric field $E_i^o$ and nominal electric displacement $D_i^o$, via a free energy $H(\lambda, E_i^o)$ as [31]:

$$S_i = \frac{\partial H}{\partial \lambda_i} + q \frac{1}{\lambda_i},$$  \hspace{1cm} (A1)

$$\frac{\partial H}{\partial E_i^o} = -D_i^0,$$  \hspace{1cm} (A2)

where $q$ is a pressure term defined by boundary conditions.

These forms are implied by the expression of the change $\dot{H}$ of $H$ brought about by independent changes $\dot{\lambda}_i$ and $\dot{E}_i^o$

$$\dot{H} = S_i \dot{\lambda}_i + q \frac{\lambda_i}{\lambda_i} - D_i^0 \dot{E}_i^o.$$  \hspace{1cm} (A3)

As shown by isotropic finite-strain electro-mechanics, along principal axes $E_i^o=[\epsilon E_i]$, $D_i^o=[\sigma D_i]$ and $S_i=[\sigma \lambda_i]$, so that introducing the function $W(\lambda_i, E_i) = H(\lambda_i, [\lambda E_i])$, it turns out that eq. (A3) is equivalent to

$$\frac{\partial W}{\partial \lambda_i} \dot{\lambda}_i + \frac{\partial W}{\partial E_i} \dot{E}_i = \left[ \frac{\epsilon}{\lambda_i} \right] \dot{\lambda}_i + q \frac{1}{\lambda_i} - \left[ \frac{\sigma}{\lambda_i} \right] \left\{ \left[ \lambda E_i \right] \dot{\lambda}_i + \left[ \lambda \dot{E}_i \right] \right\}.$$  \hspace{1cm} (A4)

which corresponds to

$$\frac{\partial W}{\partial \lambda_i} = -D_i \dot{\lambda}_i$$  \hspace{1cm} (A5)

$$\frac{\partial W}{\partial E_i} = \left[ \frac{\epsilon}{\lambda_i} \right] + q \frac{1}{\lambda_i} - \left[ \frac{\sigma}{\lambda_i} \right] E_i.$$  \hspace{1cm} (A6)

In particular, (A6) can be rewritten as

$$\sigma_i = \lambda_i \frac{\partial W}{\partial \lambda_i} - q + D_i E_i \text{ (no sum on index } i),$$  \hspace{1cm} (A7)

which is employed in section VI.B.

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