gl2vec: Learning Feature Representation Using Graphlets for Directed Networks

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Abstract—Learning network representation has a variety of applications, such as network classification. Most existing work in this area focuses on static undirected networks and does not account for presence of directed edges or temporal changes. Furthermore, most work focuses on node representations that do poorly on tasks like network classification. In this paper, we propose a novel network embedding methodology, gl2vec, for network classification in both static and temporal directed networks. gl2vec constructs vectors for feature representation using static or temporal network graphlet distributions and a null model for comparing them against random graphs. We demonstrate the efficacy and usability of gl2vec over existing state-of-the-art methods on network classification tasks such as network type classification and subgraph identification in several real-world static and temporal directed networks. We argue that gl2vec provides additional network features that are not captured by state-of-the-art methods, which can significantly improve their classification accuracy by up to 10% in real-world applications.

I. INTRODUCTION

Networks, where elements are denoted as nodes and their interactions are denoted as edges, are fundamental to the study of complex systems [21], including social, communication, and biological networks. Analysis of such networks include network classification, community detection and so on. This often involves applying machine learning techniques to these problems, which requires the network to be represented as a feature vector. However, representing a network is challenging due to high dimensionality and network structure.

Various ways of learning feature representations of nodes in networks have been recently proposed to exploit their relations to vector representations [1], [9], [20], [28], [29]. However, most of these are applied to node and edge predictions and fail to fully capture network structures. It is still unclear if the result of network classification by these node embedding methods can be improved, since the whole network structure also plays a significant role. Furthermore, typical analysis usually models these systems as static undirected graphs that describe relations between nodes. However, in many realistic applications, these relations are directional and may change over time [12], [15], [29]. Modeling these directed and temporal properties is of additional interest as it can provide a richer characterization of relations between nodes in networks.

In this paper, we address the aforementioned issues by proposing a novel network embedding methodology, gl2vec, for network classification in both static and temporal directed networks. gl2vec constructs vectors for feature representations by comparing static or temporal network graphlet statistics in a network to random graphs generated from different null models (subgraph ratio profile, i.e., SRP, see Section III). Graphlets are small non-isomorphic induced subgraphs representing connected patterns in a network and their frequency can be used to assess network structures. For example, Figure I shows triads (Left), and all possible 2-node and 3-node, 3-edge, δ-temporal graphlets (Right). These will be described in detail in Section III. We show that the ratios of occurrences of graphlets in a network in comparison to random graphs (SRPs) can be used as a fixed length feature representation to classify and compare networks of varying sizes and periods of time with high accuracy. We apply various well-known machine learning models along with our graph feature representation for network classifications, and make a comparison with state-of-the-art methods, such as different graph kernels [29], node2vec [9], struc2vec [28], sub2vec [1], graph2vec [20], for network classification. We argue that gl2vec provides
additional network features that are not captured by state-of-the-art methods, which can significantly improve classification accuracy. Highlights of our contributions include:

1) We propose a novel graphlet feature representation method, gl2vec, for network classification in both static and temporal directed networks.
2) We empirically evaluate gl2vec against state-of-the-art methods on tasks such as network type classification and subgraph identification in several real-world static and temporal datasets. We find that gl2vec outperforms state-of-the-art methods in these two tasks.
3) More importantly, we show that when gl2vec is concatenated with state-of-the-art methods, the concatenation provides a significant improvement on classification accuracy in real-world applications from several domains, showing the utility of gl2vec further.

II. PROBLEM FORMULATION

In this section, we provide definitions used in the rest of the paper and formulate the problem being addressed. For temporal networks and temporal network graphlets, we consider definitions given in [26], although we can equally use definitions in [15]. We present them here for completeness.

Definition 1. A temporal directed network [25] is a set of nodes and a collection of directed temporal edges with a timestamp on each edge. Formally, a temporal directed network \( T \) on a set of nodes \( V \) is a collection of tuples \(( u_i, v_i, t_i)\), \( i = 1, \ldots, N \), where \( N \) is the number of directed temporal edges, \( u_i, v_i \in V \) and \( t_i \in \mathbb{R} \) is a timestamp. We refer to \(( u_i, v_i, t_i)\) as a temporal edge.

To strictly order the tuples, we assume timestamps \( t_i \) are unique. This assumption can be easily extended to cases where timestamps are not unique at the cost of complex notation.

Definition 2. A directed static network \( G(V, E) \) is defined as a set of nodes, denoted as \( V \) and a set of directed edges without timestamps, denoted as \( E \subseteq V^2 \setminus \{(u, u) : u \in V\} \).

Definition 3. Graphlets are small connected non-isomorphic induced subgraphs of a larger network.

In particular, we focus on triads, (see Figure 1 (Left)). The first three triads are not connected, hence do not satisfy the graphlet definition, but we argue that they are also important in constructing vectors for network feature representation.

Definition 4. Temporal network graphlets [26] are defined as induced subgraphs on sequences of temporal edges. Formally, a \( k \)-node, \( l \)-edge, \( \delta \)-temporal graphlet is a sequence of \( l \) edges, \( M = (u_1, v_1, t_1), \ldots, (u_l, v_l, t_l) \) that are time-ordered within a duration \( \delta \), i.e., \( t_1 < \cdots < t_l \) and \( t_l - t_1 \leq \delta \), such that the induced static graph from edges is connected with \( k \) nodes.

Problem Formulation: Denote \( \{G_i(V_i, E_i, L_i)\}_{i=1}^{N} \) as (sub)graphs in different static or temporal networks, where \( V_i \) is a set of nodes and \( E_i \) is a set of edges in \( G_i \). If \( G_i \) is a temporal network, \( E_i \) is then a temporal edge with a timestamp as defined in Definition 1 otherwise, \( E_i \) is a directed edge. Suppose that graphs can be categorized into \( D \) classes, \( D < N \). We associate each graph \( G_i \) with a label \( L_i \in \{1, \ldots, D\} \).

Let \( f : \{G_i\} \rightarrow \mathbb{R}^m \) be a mapping function (also called graph embedding function) from \( G_i \) to a \( 1 \times m \) feature representation vector defined using SRPs of static or temporal graphs. We formally define SRP in Section III.

Let \( g : \mathbb{R}^m \rightarrow P \in \mathbb{R}^D \) be a classifier that maps a feature representation to a categorical distribution \( P \) for \( D \) labels. We represent probability distribution of \( G_i \)'s label as \( P_i = [p_i, 1, \ldots, p_i, D] = g(f(G_i)) \).

Our goal is to solve this classification problem by designing an embedding function \( f \) and selecting a machine learning model \( g \) that minimizes the sum of cross entropy [6] for all graphs.

\[ \arg \min_{g,f} \left( -\sum_{i=1}^{D} L_i \log(p_{i,L_i}) \right) = \arg \min_{g,f} \left( -\sum_{i=1}^{D} \log(p_{i,L_i}) \right). \]

We obtain \( g \) by training machine learning models. In the next section, we discuss how to design an embedding function \( f \) for static and temporal networks using graphlets.

III. NETWORK EMBEDDING USING GRAPHLET

Network embedding has received considerable attention due to its effect on network classification, see Section V. However, previous work has primarily focused on examining this for undirected static networks. Applying these techniques to directed static networks may lose network structure information, while applying them to temporal networks loses temporal information, and both may result in poor accuracy. Therefore, we introduce a new static (temporal) network embedding technique based on static (temporal) network graphlets.

Graph embeddings need to be independent of network size and, if temporal, the time period the network covers. While previous work shows that the counting and probability distribution of graphlets are strongly related to network types [26], graphlet counts may differ across networks. Instead, we use subgraph ratio profile (SRP) for network embedding, which is computed using graphlet counts from both the network in question and random graphs produced using a null model.

Definition 5. A null model [23] is a generative model used to generate random graphs that matches a specific graph in some of its structural features such as the degrees of nodes or number of nodes and edges.

For static networks, we consider the null model for random graphs with the same number of nodes and edges (NE). NE has been widely used in previous studies since it is easy to generate random graphs [16] and the probability of a node degree in a random graph can be approximated by Poisson distribution in the large limit of graph size [24]. Thus network features and graphlet statistics can be easily modeled.

For temporal networks, since there is no equivalent null model, we consider ensembles of randomized time-shuffled data as a temporal null model [18]. To be more specific, we
randomly permute the timestamps on the edges while keeping the node pairs fixed. This model breaks the temporal dependencies between edges but preserves the network structure.

In our study, we use a null model to compare graphlet counts in a network against random graphs. The difference between counts is then used to construct an SRP as a feature representation of the network.

**Definition 6.** Subgraph ratio profile (SRP) \([19]\) for a graphlet \(i\) is defined as \(\text{SRP}_i = \frac{\Delta_i}{\sqrt{\sum_{i} \Delta_i^2}}\), where \(\Delta_i = \frac{N_{ob_i} - \langle N_{rand_i}\rangle}{\frac{1}{2}N_{ob_i} - \langle N_{rand_i}\rangle + \epsilon}\). Here \(N_{ob_i}\) is the count of graphlet \(i\) observed in an empirical network, and \(\langle N_{rand_i}\rangle\) is the average count of graphlet \(i\) in random networks in a null model. Last, \(\epsilon\) (usually set to four) is an error term to make sure that \(\Delta_i\) is not too large when a graphlet \(i\) rarely appears in both empirical and random graphs.

A large positive value of an SRP indicates that a graphlet occurs much more frequently in a network than expected by random chance. Since SRP for a graphlet has been normalized, it can be used to compare different size networks. The network embedding is a vector containing 16 SRPs for static triads and 36 for temporal graphlets as illustrated in Figure 1 (Right).

**Algorithm:** gl2vec works as follows: given the topological structure of a directed static or temporal network, we first compute its graphlet counts. For static networks, we used JMotif \([32]\) to compute triad counts for networks and random graphs in different null models. For temporal networks, we use the SNAP package \([26]\) to compute 3-edge, \(\delta\)-temporal graphlet counts. Then we compute average graphlet counts in null models \(NE\). For static networks, there are two approaches: simulation based and probability based. The simulation based approach generates a large set of random graphs with the same structure of the given network and a graphlet counts are computed for each random graph. The probability based approach computes the probability of occurrence for each type of graphlet given the in/out degree of the nodes involved. We apply the probability based approach to \(NE\) due to its fast computation speed and high accuracy. For temporal networks, we generate random graphs by shuffling timestamps on edges and then compute their average temporal graphlet counts. Finally, we compute SRPs for corresponding graphlets.

**IV. EXPERIMENTS**

In this section, we conduct network classification on several real-world static and temporal directed networks. We define two tasks, network type classification and subgraph identification, to assess the performance of gl2vec in comparison to the state-of-the-art.

**A. Datasets**

We use a wide range of real-world network datasets, which only contain topological structure. Attributes of nodes and edges are unknown, except for labels for classification, and timestamps of edges, in temporal networks. These datasets may challenge some current state-of-the-art methods that require attributes of nodes or edges.

1) **Static directed network datasets:**

**SNAP datasets \([17]\):** We use datasets from social networks, Twitter dataset, Google+ dataset, question-answering networks Askubuntu and Mathoverflow, peer-to-peer file sharing networks p2p-Gnutella, physics paper citation networks Cit-HepPh and Cit-HepTh, and so on. Due to space constraints, properties of these datasets are given in \([33]\).

2) **Temporal directed network datasets:**

**Email Networks:** EmailEU \([37]\) is a directed temporal network constructed from email exchanges in a large European research institution for a 803-day period. There are 42 ground truth departments in the dataset and we choose 26 departments whose email network sizes are larger than 10. We constructed temporal subgraphs, each lasting 12 weeks for departments in EmailEU networks. This ensures each subgraph becomes a connected network component when converted to an unweighted static graph. We create these graphs at the beginning of every four weeks to avoid too much overlap of edges between graphs. Each department has up to 28 subgraphs as a result. We also consider EmailTraffic \([25]\) in details in \([33]\).

**SwitchApp:** \([34], [35]\) is a set of networks representing application switching data for 53 Android users over a 42-day period. We construct a directed temporal network for each user on each day, where a directed edge (denoted as \(e_{uv}\)) along with a timestamp \(t\), represents a user switching from an app \(u\) to another \(v\) at time \(t\).

**B. Experiment Setup**

We compute SRPs for static and temporal graphlets for corresponding static and temporal networks in our datasets. We use three widely used machine learning models that provide good performance using small amounts of training data in multi-class classification: XGBoosting \([3]\), SVM \([4]\), and random forest \([30]\). XGBoosting usually has a superior performance over other classifiers when the dataset is of middle size. SVM is suitable for a small amount of training data. Random forest not only works well for imbalanced data, but also performs feature selection during training which can help us investigate the usefulness of our feature representation, especially when used in conjunction with other approaches by concatenating the feature vectors.

We use grid search method to search the best hyper-parameters for these models. For XGBoosting algorithm, the learning rate ranges from 0.001 to 1, maximal tree depth range from 4 to 32, minimal child weight is 1 and the subsample ratio of train instances ranges from 0.4 to 1. The regularization weight in SVM ranges from 1 to 8. In random forest, the number of trees ranges from 50 to 400 and the minimal number of samples required to split a tree node from 2 to 10. 10-fold cross-validation is adopted to split the data to select the best parameters. All experiments are conducted using a cluster with 32 Xeon CPUs, 256GB RAM and one Tesla K40 GPU.

We compare the network classification accuracy of gl2vec with state-of-the-art methods, including graphlet and Weisfeiler-Lehman kernels \([29]\), and node and graph em-
bedding methods node2vec [9], struc2vec [28], sub2vec [1], graph2vec [20].

For node embedding methods node2vec and struc2vec, we apply a sum-based approach [5] to aggregate node embedding vectors to construct a graph embedding. We refer interested readers to [11] for more detail. The length of the network embedding (ranging from 50 to 500) is determined using grid search and 10-fold cross-validation. We modify state-of-the-art methods to apply them to directed graphs: we run a random walk on directed graphs in node2vec instead of an undirected graph. Some state-of-the-art methods also require node attributes for network embeddings and node degree are suggested for computing undirected graph embedding [11]. For directed networks, we use NetworkX to compute the in/out degree and centralities such as betweenness, closeness and in/out degree centrality for each node. We also consider additional attributes: counts of subgraphs of a specific triad that a node belongs to. These counts are normalized as a distribution indicating the likelihood a node belongs to a specific triad.

C. Network Type Classification

In network type classification, we are given the topological structure of a subgraph in a network. Our goal is to predict the type of interaction that an edge represents, e.g. email exchange or question answering.

Among all the datasets introduced in Section IV-A EmailEU, EmailTraffic and SwitchApp datasets have ground truth labels (department ID or user ID) available for each subgraph, which is created from email exchanges in a department or app switch behaviors of a user within a period of time. Hence, we can obtain all subgraphs for these communities in these three networks. For the other datasets, there is no ground truth information on network communities; we detect network communities using modularity [22] to obtain subgraphs. These subgraphs are converted into feature vectors using the previously introduced embedding methods and assigned labels according to network types. Finally, we collect about 10,000 (sub)graphs from 2,355 real-world networks taken from 15 network types introduced above, which include Google+ and Twitter in social networks, high energy physics theory citation networks, Gnutella P2P networks, SwitchApp and so on.

1) Static Directed Network: We use all datasets to evaluate embedding methods on static networks. Note that we convert temporal networks into unweighted static networks by removing the timestamps on the edges. The accuracies of different embedding methods for network type classification are presented in Table I. We make the following observations:

- The machine learning methods used also have an impact on the results. For this task, XGBoost provides the best performance on average in network type classification. Although sub2vec is robust across all three machine learning models, gl2vec achieves the highest mean accuracy overall.
- We also combine gl2vec with other methods by directly concatenating their feature representation vectors. We observe a significant improvement on these methods, especially for sub2vec and struc2vec. This suggests that a combination of approaches is the most suitable, as together they capture different, important features. Furthermore, there are also improvements on MotifDist and GK Graphlet. This indicates that adding null models to construct feature representations via SRPs helps improve performance. Finally, as representations from gl2vec, MotifDist and GK Graphlet all construct features from graphlets, the improvement that gl2vec brings is not as notable.

<table>
<thead>
<tr>
<th>Embedding</th>
<th>XGBoost (%)</th>
<th>SVM (%)</th>
<th>RF (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>GK Graphlet</td>
<td>78.94 ± 3.18</td>
<td>72.66 ± 2.79</td>
<td>78.72 ± 3.01</td>
</tr>
<tr>
<td>+gl2vec</td>
<td>82.18 ± 2.86</td>
<td>69.01 ± 2.27</td>
<td>81.39 ± 3.36</td>
</tr>
<tr>
<td>GK WL</td>
<td>78.26 ± 2.65</td>
<td>72.81 ± 2.74</td>
<td><strong>78.41 ± 3.02</strong></td>
</tr>
<tr>
<td>+gl2vec</td>
<td>82.54 ± 2.85</td>
<td>68.59 ± 2.75</td>
<td>82.26 ± 3.43</td>
</tr>
<tr>
<td>MotifDist</td>
<td>78.08 ± 3.34</td>
<td>71.40 ± 2.29</td>
<td>78.01 ± 3.56</td>
</tr>
<tr>
<td>+gl2vec</td>
<td>81.75 ± 3.48</td>
<td>69.70 ± 3.64</td>
<td>80.95 ± 3.63</td>
</tr>
<tr>
<td>node2vec</td>
<td>74.25 ± 3.07</td>
<td>69.03 ± 1.23</td>
<td>72.24 ± 1.67</td>
</tr>
<tr>
<td>+gl2vec</td>
<td>88.76 ± 1.26</td>
<td>73.24 ± 2.92</td>
<td>86.14 ± 1.71</td>
</tr>
<tr>
<td>graph2vec</td>
<td>72.48 ± 3.99</td>
<td>70.81 ± 3.84</td>
<td><strong>72.61 ± 3.36</strong></td>
</tr>
<tr>
<td>+gl2vec</td>
<td>79.83 ± 4.59</td>
<td>66.70 ± 4.04</td>
<td>80.03 ± 4.38</td>
</tr>
<tr>
<td>sub2vec</td>
<td><strong>81.39 ± 1.70</strong></td>
<td>79.69 ± 1.41</td>
<td>78.44 ± 2.26</td>
</tr>
<tr>
<td>+gl2vec</td>
<td>92.30 ± 2.29</td>
<td>83.16 ± 2.62</td>
<td>90.91 ± 2.16</td>
</tr>
<tr>
<td>struc2vec</td>
<td>79.15 ± 3.42</td>
<td>78.22 ± 3.15</td>
<td>78.94 ± 3.31</td>
</tr>
<tr>
<td>+nodeTriadDistr</td>
<td>81.93 ± 3.53</td>
<td>79.18 ± 3.55</td>
<td>82.01 ± 3.42</td>
</tr>
<tr>
<td>+gl2vec</td>
<td>93.38 ± 1.51</td>
<td>84.25 ± 0.82</td>
<td>93.48 ± 1.42</td>
</tr>
<tr>
<td>gl2vec</td>
<td><strong>81.58 ± 3.07</strong></td>
<td>71.64 ± 2.13</td>
<td>79.42 ± 3.69</td>
</tr>
</tbody>
</table>

Table I: Network type classification accuracy. We use “+” to denote an embedding generated by combining two embedding methods. Bold indicated best performance machine learning model for each embedding.

- The graph-based network embedding methods, GK Graphlet, sub2vec, gl2vec, and struc2vec with added subgraph features (triad distribution for a node), have a larger average accuracy compared to other node-based network embedding methods. This further validates the importance of including subgraph information into feature representations for tasks like network classification in which network structure plays a significant role.

2) Temporal directed network: We explore if temporal graphlets provide more information than static graphlets in temporal networks. We investigate their effect on predicting...
whether a temporal (sub)graph is an email exchange network, or the app switching behavior of a mobile user. The results are shown in Figure 2. From Figure 2, we observe that temporal information improves network type classification in all models considered here. Therefore, it is important to use temporal graphlets for constructing vectors for feature representations of temporal networks, since they capture more of the network dynamics than static graphlets.

**D. Subgraph Identification**

In subgraph identification, we are interested in classifying subgraphs within the same network given their topological structure. For example, we can identify which department an email exchange subgraph belongs to or detect a mobile phone user given their app switching behavior.

We use EmailEU, EmailTraffic and SwitchApp datasets since ground truth labels (department ID or user ID) are available for each subgraph, which is created from email exchanges within a department or by the app switch behavior of a user within a period of time. We first solve this problem using static graph embedding methods. Then we investigate whether the timestamp information of edges can help improve identification accuracy.

1) **Static directed networks:** Due to space constraints, we only present results on the accuracy of identifications of departments in EmailEU in Tables II and direct the reader to [33] for results for EmailTraffic and SwitchApp networks. Overall, we note that gl2vec with a random forest model outperforms the other methods in terms of mean accuracy. Additionally, combining graphlet SRP features with the other methods results in a notable performance increase across the different machine learning models.

More broadly, we note that from Table II random forest (RF) models are usually more accurate for graph embeddings that include our SRP feature vectors in baselines. This is because RF automatically performs feature selection during training and adapts to the change in number of features. As a result, it is easier for RF to achieve better results given a similar amount of effort fine-tuning the hyper-parameters.

**2) Temporal directed networks:** In temporal networks from EmailEU and EmailTraffic, we attempt to identify which department emails belong to. For the SwitchApp dataset, we attempt to identify a particular user based on their daily app switching behavior represented as a temporal network.

For the EmailEU and EmailTraffic dataset, multiple temporal and static networks are constructed for each department from email exchanges as described in Section IV-A2. For the SwitchApp dataset, 42 temporal and static networks are generated for each person from their app switching behaviors every day. XGBoosting, SVM and random forest are implemented using different network feature representations: SRP with temporal (“Temporal”) graphlets, SRP with static (“Static”) graphlets, and a combination of both (“Temp+Static”). We illustrate the result from sub2vec representation (“Sub2Vec”) because it performs best among the baseline methods and create a combination of all three representations (“CombineAll”).

Results for EmailEU is shown in Figure 3 and as with static networks, results for EmailTraffic and SwitchApp can be found in [33]. The dashed line is the accuracy of a random selection model. We note that the combination of static and temporal graphlet features (“Temp+Static”) produces an improvement in accuracy over each set of features individually. Additionally, our graphlet-based network embeddings are competitive against the state-of-the-art method, sub2vec. However, combining all three graph embedding vectors for classification yields the best accuracy. Overall, the results highlight that graphlet-based features capture important characteristics for network classification tasks.

**V. RELATED WORK**

The primary focus of related works in classifying networks involves examining the topological structure of the graph. The work most related to our method is graph kernels, which has been used to calculate similarities between static undirected graphs [13], [36]. However, the corresponding computational complexity grows significantly with increases in network size. Moreover, studies surrounding graphlet kernels do not consider features generated by comparing graphlet count between an empirical network and random graphs from different null models, which we find leads to notable improvements in network classification tasks in our experiments.
Different node embedding techniques have been proposed in recent years, such as node2vec \cite{10}, DeepWalk \cite{27}, and Line \cite{31} that use feature vectors to embed nodes into high-dimensional space and empirically perform well. However, these methods are focused on node classification rather than graph classification. Additionally, neural networks \cite{7}, \cite{14} recently obtained competitive results against kernel-based methods and graph-based regularization techniques, but they are computationally expensive and typically used only for small scale tasks.

Additionally, several approaches have been proposed to aggregate node feature vectors to a feature vector for networks. For example, a graph-coarsening approach \cite{7} computes a hierarchical structure containing multiple layers, nodes in lower layers are clustered and combined as node in upper layers using element-wise max-pooling. However, this has high computational complexity. Recently, subgraph embedding based approaches have been proposed. \textit{struc2vec} \cite{28} applies a sum-based approach such as mean-field and loopy belief propagation to aggregate node embedding to graph representation. \textit{sub2vec} \cite{1} embeds subgraphs with arbitrary structure, while \textit{graph2vec} \cite{20} was proposed based on a doc2vec framework to learn data-driven distributed representations of arbitrary sized graphs. However, these embedding techniques do not fully capture the network structure. Similar to ours is \cite{2}, which uses motif frequencies, while we use graphlet distributions and SRP. Furthermore, \cite{2} also requires node labels in its use of network motifs, but we do not.

VI. CONCLUSION

We introduce \textit{gl2vec}, a methodology for classifying static and temporal directed networks based on graphlet features their topological structure. Experiments with real-world datasets have shown that both temporal and static graphlets are important features for network type classification and subgraph identification tasks in comparison to state-of-the-art methods. Furthermore, we have illustrated that concatenating these two types of features with many state-of-the-art methods yields further accuracy improvements.

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