LDA+DMFT approach to electronic structure of sodium metal

L. Craco\(^1\) and S. Leoni\(^2\)

\(^1\)Instituto de Física, Universidade Federal de Mato Grosso, 78060-900, Cuiabá, MT, Brazil
\(^2\)School of Chemistry, Cardiff University, Cardiff, CF10 3AT, United Kingdom

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Based on local density approximation plus dynamical mean-field theory (LDA+DMFT) calculations, we revisit the long-standing quasiparticle band narrowing problem of sodium metal. Using an on-site Coulomb interaction \(U\) derived from angle-resolved photoemission spectroscopy mass enhancement, we can describe various properties of this weakly correlated electron system. Intrinsic self-energy corrections lead to a Landau-Fermi liquid state with many-particle coherence and dynamical spectral weight transfer relevant to electronic structure and scattering rates of alkali metals.

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I. INTRODUCTION

Sodium traditionally has been considered to be one of the best realizations of nearly-free-electron gas that can be found in three-dimensional solid state crystals. Its electronic structure has been studied for more than 80 years. \([1]\) Historically, angle-resolved photoemission spectroscopy (ARPES) experiments by Plummer \textit{et al.} \([2,3]\) pointed out that the quasiparticle dispersion curve for the occupied bands of Na is remarkably narrowed in comparison with the usual value obtained from band-structure calculations \([1]\). This remarkable result was corroborated by x-ray absorption (XAS) \([4]\) experiments showing a substantially smaller unoccupied bandwidth than that predicted by band-structure calculations: This discrepancy is linked to the fact that spectroscopy measurements probe the excitation spectra while band-structure calculations (based, for example, on local density approximation, LDA) \([5]\) describe ground-state properties \([3]\). Motivated thereby, a number of studies \([3,6–8]\) have been conducted to understand the quasiparticle band narrowing of Na in terms of self-energy corrections due to many-body effects. However, a conclusive answer to this problem has not yet been found in spite of many different efforts \([9–14]\).

In this paper, we report correlated band-structure calculations for the contribution of self-energy corrections arising from local Coulomb interactions. Namely, we employ the LDA plus dynamical mean-field theory (LDA+DMFT) formalism \([15]\) for the multiband, multiorbital (MO) problem of Na. We use the iterated perturbation theory (IPT) impurity solver \([16,17]\) to DMFT, showing the role played by the local Coulomb repulsion to intrinsic bandwidth reduction of both valence and conduction band states of Na. Our results attest that the electronic states near the Fermi energy \(E_F\) probed by photoemission and inverse photoemission experiments \([2–4,10]\) are narrowed under the influence of sizable on-site Coulomb interactions responsible for low-energy quasiparticle excitations in solid Na.

We shall first point out here the study by Dolado \textit{et al.} \([12]\), which finds only small momentum dependence on calculated lifetimes of Na at different \(k\)-directions and approximately quadratic energy scaling characteristic of Landau-Fermi liquid metals. Also relevant to our proposal is the work by Lyo and Plummer \([3]\), which argues that local-field corrections must be included in random-phase approximation (RPA) calculations to correctly reproduce the quasiparticle band shape of Na. With this caveat in mind, in this paper, we show that dynamical electronic correlations hidden in the local, momentum-independent self-energy \(\Sigma(\omega)\) play a significant role for the quasiparticle band narrowing and electronic mass enhancement of Na and related nearly free alkali systems.

On general grounds, for Landau-Fermi liquid metals, the renormalized band structure can be written as \(\varepsilon^\ast(k) = \varepsilon(k)Z\overline{Z}\) \([18]\), where \(Z = (1 - \frac{\partial \Sigma(\omega,k)}{\partial \omega})^{-1}\) and \(\overline{Z} = (1 + \frac{\partial \Sigma(\omega,k)}{\partial \omega})\). Here, \(\nu_F\) and \(k_F\) are, respectively, the Fermi velocity and Fermi momentum. Since in DMFT the self-energy is momentum independent, the quasiparticle residue \(Z\), which defines the renormalized Fermi energy, directly yields the effective mass of quasiparticles \([19]\): \(m^\ast/m = \frac{1}{Z} = (1 - \frac{\partial \Sigma(\omega)}{\partial \omega})\). Thus, in DMFT, the effective mass ratio \(m^\ast/m\) and \(Z\) are both directly related to the slope of \(\Sigma(\omega)\), and the many-particle band renormalization is therefore solely given by the product between the bare-band dispersion \(\varepsilon(k)\) and quasiparticle amplitude \(Z(\omega = 0) = Z(0)\).

The possibility of correlated electron physics in purely \(p\) \([20,21]\) or \(s\) \([22]\) band systems is intriguing, since the naive expectation dictates that the itinerancy (kinetic energy of \(p, s\) carriers) is appreciable compared to the electron-electron interactions, as distinct from \(d\)-band systems, where the \(d\) electrons reside in much narrower bands. Thus, understanding the role of electron-electron interactions in materials with active \(p\) or \(s\) bands is undoubtedly an issue of great contemporary interest. In light of the discussion above, we study how an interplay between appreciable \(s-, p\)-band itinerancy and on-site Coulomb repulsion, \(U\), plays a central role in the quasiparticle band narrowing of Na.
temperature free-electron gas (FEG) concepts, where \( \epsilon(k) = \frac{\xi^2}{2} k^2 \) and \( Z_0 = 1 \). With this in mind, and focusing on Na, here we carried out a comprehensive numerical study of electron correlations effects, providing a compelling theoretical evidence of local self-energy corrections to the bare LDA band structure. We use LDA+DMFT [15] to address this long-standing problem of fundamental importance.

Within LDA, the one-electron part of the two-channel model Hamiltonian relevant to Na is \( H^0 = \sum_{\alpha\beta\sigma} \epsilon_\alpha(k) c_{\alpha\sigma}^\dagger(k) c_{\alpha\sigma}(k) \), where \( \alpha \) denotes the 3s and 3p bands crossing \( E_F \) [1]. Here, \( \epsilon_\alpha(k) \) is the two-channel band dispersion, which encodes details of the one-electron (LDA) band structure. These \( s \) and \( p \) bands are the relevant one-particle inputs for correlated band-structure calculations within LDA+DMFT. In light of non-negligible correlation effects in Na, here we show how a DMFT treatment of many-particle Coulomb interaction effects properly describe the onset of correlated responses seen in the spectral function of Na. This constitutes the one- [25] and MO [15] local interaction terms \( H^\text{int}_{\alpha} \) and \( H^\text{int}_{p} \), respectively. The correlated many-body Hamiltonian \( H^{\text{int}} = H^0 + H^\text{int}_{\alpha} + H^\text{int}_{p} \) considered for Na thus reads

\[
H^{\text{int}} = U \sum_{\sigma} n_{\alpha\uparrow} n_{\alpha\downarrow} + U \sum_{\sigma} n_{p\sigma} n_{p\sigma} - J_H \sum_{\alpha\beta\sigma\tau} \mathbf{S}_{p\alpha\sigma} \cdot \mathbf{S}_{p\beta\tau}.
\]

Here \( \alpha = x, y, z \) denotes the diagonalized 3p orbitals, \( U \) is the on-site Coulomb interaction, \( U' = U - 2J_H \) is the interorbital p-band Coulomb interaction term, and \( J_H \) is the corresponding Hund’s coupling. Consistent with earlier studies [26], we focus on the leading local correlation effects and will not consider the pair-hopping term in the MO p-band problem of Na for simplicity [27]. We evaluate the many-particle Green’s functions,

\[
G_{\alpha\sigma}(\omega, k) = \frac{1}{\omega - \Sigma_{\alpha\sigma}(\omega) - \epsilon_\alpha(k)},
\]

of the many-body Hamiltonian \( H = H^0 + H^{\text{int}} \) using one-band [16] and MO [17] IPT impurity solvers for \( H^{\text{int}}_{\alpha} \) and \( H^{\text{int}}_{p} \), respectively.

On general grounds for nonmagnetic electronic systems, the many-particle Green’s function of an orbital \( \alpha \) can be computed using the following relation for the MO-IPT self-energy [17]:

\[
\Sigma_{\alpha}(\omega) = \sum_{\beta} \left[ N_{\alpha\beta} U_{\alpha\beta} \langle n_\beta \rangle + A_{\alpha\beta} \frac{\Sigma_{\alpha}^{(2)}(\omega)}{1 - B_{\alpha\beta} \Sigma_{\alpha}^{(2)}(\omega)} \right],
\]

with \( \Sigma_{\alpha}^{(2)}(\omega) = N_{\alpha\beta} \frac{U_{\alpha\beta}}{\pi \nu} \sum_{i\sigma} G_{\alpha\sigma}^{\text{int}}(i\omega_n) G_{\beta\sigma}^{\text{int}}(i\omega_n) G_{\beta\sigma}^{\text{int}}(i\omega) \) being the second-order (in \( U_{\alpha\beta} \)) contributions and \( N_{\alpha\beta} = 2 - \delta_{\alpha\beta} \). In contrast to the usual one-band Hubbard model [16], the atomic limit for the MO case contains local, interorbital correlation functions, \( D_{\alpha\beta} \) [28]. The equations for the parameters \( A_{\alpha\beta} \) and \( B_{\alpha\beta} \) are explicit functions of \( U_{\alpha\beta} \), \( D_{\alpha\beta} \), and the average numbers (per spin \( \sigma \)) \( \langle n_\alpha \rangle \equiv \langle n_{\alpha\uparrow} \rangle + \langle n_{\alpha\downarrow} \rangle \) [29]. The latter is the effective number of fermions in the \( \alpha \) orbital corresponding to site-excluded Green’s function.

L. CRACO AND S. LEONI
PHYSICAL REVIEW B 100, 115156 (2019)
The IPT ansatz is known to account for the correct low- and high-energy behavior of the one-particle spectral functions and self-energies of one-band [19] and MO models [17,30] in the large dimensional limit (DMFT). It ensures the Mott-Hubbard metal-insulator transition from a correlated metal to a Mott insulator as a limit (DMFT). It is worth noting here that the IPT ansatz is known to account for the correct low- and high-energy behavior of the one-particle spectral functions and self-energies of one-band [19] and MO models [17,30] in the large dimensional limit (DMFT). It ensures the Mott-Hubbard metal-insulator transition from a correlated metal to a Mott insulator as a limit (DMFT). It ensures the Mott-Hubbard metal-insulator transition from a correlated metal to a Mott insulator as a limit (DMFT).

For the high-symmetry body-centered cubic structure of Na, the 3s and 3p bands crossing \( E_F \) [1] were obtained using the linear muffin-tin orbital [5] scheme within the LDA [32]. In the inset of Fig. 2, we display the channel-resolved LDA density of states (DOS) used to compute the renormalized LDA+DMFT spectral functions of solid Na. As expected for \( s \) and \( p \) band systems, the LDA DOS of Na is broad, with a bare bandwidth of \( W \approx 14.5 \) eV. Consistent with early band-structure calculations [1], the width of the valence band is close to 3.2 eV. Interestingly as well is the line shape of the total DOS (see main panel) up to 0.4 eV above \( E_F \) which follows almost perfectly the energy dependence of a three-dimensional FEG. However, due to electron-ion interaction effects [33], deviations from this canonical text-book behavior is visible in the conduction band states above 0.4 eV. Equally interesting are the deep-hump structures between 1.2 eV and 3.0 eV above \( E_F \). As shown in the inset of Fig. 1, these structures are important for understanding the unoccupied band structure [4] of Na at low energies.

To make progress, in Fig. 3 we show the electronic reconstruction induced by local Coulomb correlation effects in the 3s (main panel) and 3p (inset) band states of Na computed using three different \( U \) values and fixed Hund’s exchange coupling \( J_H \). In view of the ambiguity regarding the importance this two-particle exchange interaction to Na [34], we use \( J_H = 0.5 \) eV as a model parameter. It is worth noting, however, that the \( U \) values considered in this paper are close to the bare Coulomb interaction \( U = 8.0 \) eV derived in Ref. [14] and this choice leads to an effective \( U_{\text{eff}} \equiv U/W \) Coulomb interaction of \( 0.55 < U_{\text{eff}} < 0.69 \), implying a weakly correlated scenario for Na metal. Indeed, our fully self-consistent LDA+DMFT (IPT) results for the half-field (one electron per site) electronic configuration of Na shows weak, albeit non-negligible, spectral weight transfer (SWT) across large energy scales. This is a fingerprint of correlated electron systems within DMFT. The dynamical nature of SWT can be characterized by Kondoesque band narrowing at energies near \( E_F \) and the presence of crossing points in the 3s valance and conduction band at \(-2.8 \) eV and \( 5.2 \) eV, respectively. Also interesting is the suppression of the \( V \) valley at 2.96 eV above \( E_F \) due large energy dynamical SWT. Moreover, the inset of Fig. 3 shows a suppression of the \( p \)-band electronic structure of Na. The lack of SWT in this orbital sector reflects its almost empty nature, and the fact that electron-electron interaction reaches its maximum at half filling and to decrease away from this configuration [35].

Our total LDA+DMFT DOS \( \rho_{\text{total}}(\omega) = \frac{1}{2} \sum_{\alpha=x,y,z} \sigma(G_{\alpha,\sigma}(\omega) + \sum_{\sigma} C_{\sigma,\alpha,\sigma}(\omega)) \) shows qualitative good agreement with x-ray photoemission spectroscopy (PES) [10,23] and K-edge absorption (XAS) [4] data. As seen in the inset of Fig. 1, both PES and XAS lineshapes are correctly reproduced by LDA+DMFT. Particularly interesting are the absorption peaks at 0.7 eV and 2.2 eV in XAS and the PES spectra up to 3.0 eV binding energy, which are correctly
reproduced in theory. Taken together, the comparison between (PES and XAS) quasiparticle band narrowing in Fig. 1 and electron mass enhancement testify the use of LDA+DMFT and the validity of the local correction for a consistent explanation of correlation fingerprints seen in the occupied and unoccupied electronic states within the energy range relevant to AC transport [1] and spectroscopy [2,3,7] experiments.

To obtain detailed information on the evolution of the correlated electronic structure of Na metal, in Fig. 4 we compare our LDA+DMFT(IPT) total DOS for two $U$ values with results obtained from adiabatic LDA (ALDA) [23], $G_0W^0$ and combined GW plus extended DMFT (GW+eDMFT) calculations [14]. As seen, good qualitative agreement is obtained using LDA+DMFT(IPT), $G_0W^0$, and GW+eDMFT implementations from $-5.0 \ eV$ binding energy up to $0.8 \ eV$ above $E_F$. Above this energy, the agreement between LDA+DMFT(IPT) and both $G_0W^0$ and GW+eDMFT treatments is lost. As compared to our LDA result, all correlated total spectral functions show band narrowing at low energies as well as downshifts of the main conduction band peak in LDA at $0.8 \ eV$ above $E_F$. Also visible is the SWT at the conduction band from low to energies above $3.2 \ eV$ binding energy.

To get additional microscopic insights into the correlated electronic structure evolution due to Landau-Fermi liquidness, in Fig. 5 we show the frequency dependence of $3s$-band self-energy real part $\Pi_\omega(\omega)$ and imaginary part $\Im \Sigma_\omega(\omega)$ parts. As seen in the main panel of Fig. 5, $\Re \Sigma_\omega(\omega)$ follows the $\omega^2$ behavior intrinsic to Landau-Fermi liquids [19] at low energies. Low-energy coherence is also reflected in the linear dependence of $\Im \Sigma_\omega(\omega)$ relevant to band mass renormalization seen in experiment [2]. Thus, taken together with earlier studies [16,17,19], our results in Fig. 5 certify the existence of low-temperature Landau-Fermi liquidness in Na at ambient pressure. However, how stable this coherent many-particle state is against nonlocal perturbations [6,8,13,36] not included in $H_{int}$ or disorder effects [16] remains to be seen. We defer this latter study, however, for a separate work.

As an additional test to our proposal and the validity of the LDA+DMFT approximation to nearly-free-electrons, in Fig. 6 we compare our results for the $3s$-band scattering rate $\Gamma_{s}(\omega) = -2\Im \Sigma_{s}(\omega)$ [37] with results based on FEG-RPA calculations of hole and electron line widths taken from Ref. [12]. As expected, both RPA and DMFT results in Fig. 6 show nearly perfect $\omega^2$ behavior characteristic of normal Landau-Fermi liquid metals [38]. In spite of different

FIG. 4. Total local density of states of Na metal obtained using LDA, LDA+DMFT, $G_0W^0$, GW+eDMFT [14], and ALDA [13] schemes. Notice the good qualitative agreement between LDA+DMFT, $G_0W^0$, and GW+eDMFT treatments at low binding energies and the high in energy satellite seen in the $G_0W^0$ and ALDA results.

FIG. 5. $3s$-band self-energy real (inset) and imaginary (main panel) parts of Na, showing intrinsic Landau-Fermi liquid energy-dependence within DMFT [19].

FIG. 6. Comparison between $3s$ LDA+DMFT and free-electron gas (FEG) RPA calculation for the quasiparticle scattering rate $\Gamma_{s}(\omega) = -2\Im \Sigma_{s}(\omega)$ (FEG-RPA results are taken from Ref. [12]). Notice the nearly perfect Landau-Fermi liquid behavior and the agreement between RPA and DMFT for electron and hole scattering rates at low energies. Inset shows the changes induced by the energy-dependence in the LDA + DMFT($U = 9.0 \ eV$) quasiparticle amplitude $Z_{s}(\omega)$ within the energy window relevant to ARPES experiments.
formulations and computation frameworks, the good low-energy FEG-RPA and LDA+DMFT agreement provides support to our model parameter choice. Importantly, and similar to what has been suggested in Ref. [3], below −0.7 eV the agreement is lost and appreciable deviations are seen at high binding energies, where the RPA quasiparticle scattering rate is considerably smaller as compared to DMFT results. This can be taken as additional evidence for the role played by dynamical, local electron-electron interactions to self-energy corrections inducing 3s electronic reconstruction. Interestingly as well is the particle-hole asymmetry found in FEG-RPA, which is well captured by LDA+DMFT, and the nice agreement between FEG-RPA and LDA + DMFT(\(U = 9.0\) eV) up to 2.6 eV above \(E_F\). However, deviations from the high-energy LDA+DMFT response are expected to be seen in future studies, particularly if additional \(k\)-dependent [6,8,13,36] scattering mechanisms not considered in our description or dynamical screening effects induced by electron-plasmon (electron-boson) interaction [39] are self-consistently taken into account. This many-body corrections to DMFT are predicted to have significant influence on the high-frequency part of the both electron- and holelike scattering rates. However, observation of similar low-energy features as shown in the inset of Fig. 6 in future ARPES experiments would be a stringent test to our Landau-Fermi liquidness scenario and the role played by sizable local electron-electron correlation effects in the electronic structure of Na.

Despite the success of the one-band Hubbard model to capture dynamical many-body properties of correlated electrons [19], including, as shown here, Na metal, it misses nonlocal Coulomb interaction terms relevant for spin- and charge-density wave instabilities [40] and plasmon physics: [13] The latter has been discussed in the context of valence-electron excitations [11] and pressure-induced increases in the electron-ion interaction [41] of alkali metals like Na, K, and Rb. In the case of Na, a plasmonic satellite feature in the experimental spectra is seen around 7 eV binding energy and Rb. In the case of Na, a plasmonic satellite feature in the electron-ion interaction [41] of alkali metals like Na, K, and Rb. The inset of Fig. 4 shows that we investigated the electronic structure of sodium metal using LDA+DMFT with sizable multi-band, MO interactions. Although the main purpose of this paper is to understand the quasiparticle band narrowing due to electron-electron interactions, a major finding of the present paper is that considerable changes in the electronic structure would be found due to dynamical SWT from low to high energies. Particularly for the 3s conduction band states, where an incipient upper Hubbard band is predicted to be seen at energies close to 5.3 eV, this is a clear manifestation that more is different [44] also to nearly-free-electron-like systems. Our Landau-Fermi liquidness approach suggests that retarded interactions stemming from collective plasmon excitations [39] play a minor role in determining the frequency dependence of quasiparticle (electron/hole) scattering rates at low energies. Future collective charge excitation studies of correlated electrons are called for to corroborate this prediction for Na metal.

III. CONCLUSION

In summary, we investigated the electronic structure of sodium metal using LDA+DMFT with sizable multi-band, MO interactions. Although the main purpose of this paper is to understand the quasiparticle band narrowing due to electron-electron interactions, a major finding of the present paper is that considerable changes in the electronic structure would be found due to dynamical SWT from low to high energies. Particularly for the 3s conduction band states, where an incipient upper Hubbard band is predicted to be seen at energies close to 5.3 eV, this is a clear manifestation that more is different [44] also to nearly-free-electron-like systems. Our Landau-Fermi liquidness approach suggests that retarded interactions stemming from collective plasmon excitations [39] play a minor role in determining the frequency dependence of quasiparticle (electron/hole) scattering rates at low energies. Future collective charge excitation studies of correlated electrons are called for to corroborate this prediction for Na metal.

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