

H-ATLAS: a candidate high redshift cluster/protocluster of star-forming galaxies

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ABSTRACT

We investigate the region around the *Planck*-detected $z = 3.26$ gravitationally lensed galaxy HATLAS J114637.9-001132 (hereinafter HATLAS12-00) using both archival *Herschel* data from the H-ATLAS survey and using submm data obtained with both LABOCA and SCUBA2. The lensed source is found to be surrounded by a strong overdensity of both *Herschel*-SPIRE sources and submm sources. We detect 17 bright ($S_{870} > \sim 7$ mJy) sources at $>4\sigma$ closer than 5 arcmin to the lensed object at 850/870 μm . 10 of these sources have good cross-identifications with objects detected by *Herschel*-SPIRE which have redder colours than other sources in the field, with 350 μm flux $> 250 \mu\text{m}$ flux, suggesting that they lie at high redshift. Submillimeter Array (SMA) observations localise one of these companions to ~ 1 arcsec, allowing unambiguous cross identification with a 3.6 and 4.5 μm *Spitzer* source. The optical/near-IR spectral energy distribution of this source is measured by further observations and found to be consistent with $z > 2$, but incompatible with lower redshifts. We conclude that this system may be a galaxy cluster/protocluster or larger scale structure that contains a number of galaxies undergoing starbursts at the same time.

Key words: galaxies: high redshift – galaxies: starburst – submillimetre: galaxies.

1 INTRODUCTION

The early history of galaxy clusters is a poorly constrained aspect of galaxy and large-scale structure formation. Hierarchical clustering models predict that massive elliptical galaxies will form in the cores of what will become the most massive galaxy clusters today, but the epoch of the bulk of star formation for these galaxies is unclear. Observations of high redshift clusters ($z = 1\text{--}1.5$) by the ISCS project (IRAC Shallow Cluster Survey; Eisenhardt et al. 2008) suggest that this is at $z > 3$, and the presence of well-defined red sequences of galaxies in clusters out to $z \sim 2$ (Andreon & Huertas-Company 2011; Gobat et al. 2011; Santos et al. 2011; Pierini et al. 2012) supports this conclusion. Theoretical models by Granato et al. (2004) suggest that forming clusters will go through a phase in

which multiple members will undergo near-simultaneous massive bursts of star formation. The spectral energy distribution of these objects would be dominated by the far-IR, as is the case for local massive starbursts (e.g. Clements, Dunne & Eales 2010). A galaxy cluster or protocluster (we use the term protocluster to indicate a structure that has yet to become virialized) going through such a formative phase would appear as a clump of dusty protospheroidal galaxies, and might be detected by observations in the far-IR and submm bands. Hints of such objects may already have been found by *Spitzer* (Magliocchetti et al. 2007) and SCUBA (Ivison et al. 2000; Priddey, Ivison & Isaak 2008; Stevens et al. 2010 and references therein). A recent study by Ivison et al. (2013) has uncovered a group of HLIRGs and ULIRGs at $z = 2.41$ thought to be the progenitor of a $10^{14.6} M_{\odot}$ cluster. At still higher redshifts, the highest redshift protocluster currently known, at $z \sim 5.3$ (Riechers et al. 2010; Capak et al. 2011), and a group of objects associated with a $z = 5$ quasar (Husband et al. 2013) both contain at least one submm-luminous

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object, while the best studied group of high z submm-luminous sources to date is probably the four objects associated with a source in the GOODS-North field designated GN20, all lying at $z = 4$ (Daddi et al. 2009; Carilli et al. 2011), though this group is extended over a broad range of redshifts $\Delta z \sim 0.1$.

Large area surveys with the *Herschel Space Observatory* (Pilbratt et al. 2010), SCUBA2 (Dempsey et al. 2013; Holland et al. 2013), or the *Planck* all sky survey (Negrello et al. 2005; Planck Collaboration XVI 2011) are capable of finding such objects. Several studies have been undertaken combining *Planck* and *Herschel* data to identify candidate high redshift clusters while others have used *Herschel* data (eg Valtchanov et al. 2013; Dannerbauer et al. 2014; Rigby et al. 2014) or SCUBA2 data (Casey et al. 2015; Ma et al. 2015) alone or in combination (Noble et al. 2013). Clements et al. (2014) found a number of candidate objects in the HerMES (Oliver et al. 2012) survey at $z \sim 1-2$, while *Herschel* followup observations of *Planck* all sky sources (Planck Collaboration XXVII 2015) have identified at least one $z \sim 1.7$ cluster of dusty galaxies and large numbers of candidates. The sources uncovered in HerMES include two clusters lying at $z \sim 0.8$ and $z \sim 2$, confirmed by the presence of a red sequence, and two lying at $z \sim 1.1$ and $z \sim 2.3$ confirmed through photometric redshift analysis. Total star formation rates for these HerMES clusters, derived from the *Herschel* fluxes of their members, range from 1000 to 10 000 $M_{\odot} \text{ yr}^{-1}$. The highest redshift candidate cluster of dusty galaxies so far, though, has emerged from analysis of *Planck* sources seen in the first release of data from the H-ATLAS survey (Herranz et al. 2013). This paper describes the results of followup observations of this source.

In the next section we describe the H-ATLAS survey and the properties of the source HATLAS J114637.9-001132 (referred to in the rest of this paper as HATLAS12-00, after Fu et al. 2012) uncovered by Herranz et al. (2013) through matching the *Planck* Early Release Compact Source Catalog (ERCSC; Planck Collaboration XVI 2011) to the Phase 1 H-ATLAS maps and catalogues (Valiante et al., in preparation). In Section 3 we describe the followup observations of this source, obtained using a variety of telescopes, together with the reduction and analysis of this data. The results of these observations are discussed in Section 4, while Section 5 discusses the nature of the sources found in these observations. Our conclusions are summarized in Section 6. Throughout this paper we assume a standard concordance cosmology with $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_M = 0.3$ and $\Omega_{\Lambda} = 0.7$.

2 H-ATLAS AND THE $z = 3.26$ LENSED SOURCE HATLAS12-00

2.1 The H-ATLAS Survey

The *Herschel* Astrophysical Terahertz Large Area Survey (H-ATLAS; Eales et al. 2010) uses the PACS (Poglitsch et al. 2010) and SPIRE (Griffin et al. 2010) instruments on the *Herschel* Space Observatory (Pilbratt et al. 2010) to survey a total of 616 deg^2 of sky, making it the largest area extragalactic survey executed by *Herschel*. PACS observations are made at 100 and 160 μm while SPIRE covers the 250, 350 and 500 μm bands. The instrumental beams have full width half-maximum (FWHM) values of 8.7, 13.1, 18.1, 25.2 and 36.9 arcsec, respectively, from 100 to 500 μm , with 5σ point source sensitivities of 132, 126, 32, 36 and 45 mJy, taking into account confusion (6–8 mJy in the SPIRE bands) and instrumental noise. Map making and data reduction for the H-ATLAS survey are discussed in detail in Pascale et al. (2011) and Ibar et al.

(2010), and source detection and catalogue generation are described in Rigby et al. (2011).

The fields covered by H-ATLAS include the Northern and Southern Galactic Poles (NGP and SGP) and three fields at $\text{DEC} \sim 0$ that were selected to match the three fields of the Galaxy And Mass Assembly (GAMA; Driver et al. 2011) survey, which provides plentiful redshifts for $z < 0.5$ optically selected galaxies. The phase 1 H-ATLAS data release includes the GAMA fields (Valiante et al., in preparation; Bourne et al., in preparation), while further data releases will cover the larger NGP and SGP survey areas. The maps that form the basis for this release are background subtracted and convolved with a matched filter (Chapin et al. 2011) calculated to produce the maximum signal to noise for sources that are unresolved in the un-smoothed images. Sources are then selected from these maps using the MADX algorithm (Maddox et al. 2010; Maddox et al., in preparation). Comparison of the results of this process for the match-filtered phase 1 catalogues and the un-match-filtered SDP catalogues (Rigby et al. 2011) show clear but modest improvements in both S/N and positional accuracy (see Valiante et al., in preparation, for more details of the data reduction methods and comparison with previous results).

2.2 The lensed source HATLAS12-00

Herranz et al. (2013) searched for cross identifications between *Planck* ERCSC (Planck Collaboration XVI 2011) and phase 1 release H-ATLAS sources (roughly 25 per cent of the final 616 deg^2). 28 matches were found, most of which were associated with nearby quiescent galaxies detected in the optical (Herranz et al. 2013) or with extended cirrus dust structures in our own Galaxy. One source, however, had no bright optical counterpart and showed no signs of cirrus contamination. The submm colours of this *Planck* ERCSC source are unusually red (see fig. 12 of Herranz et al. 2013) suggesting that it might lie at high redshift. Examination of the *Herschel* images from H-ATLAS shows that it is associated with a clump of sources, several of which have red *Herschel* colours (ie. 350 μm flux $> 250 \mu\text{m}$ flux, see below), grouped around a single bright, optically unidentified *Herschel* source, designated HATLAS12-00, whose flux peaks at 350 μm .

HATLAS12-00 had already been identified as a candidate gravitationally lensed galaxy as a result of its high submm flux (i.e. $F_{500} > 100 \text{ mJy}$), red *Herschel* colours and the lack of a bright optical or radio counterpart (see e.g. Negrello et al. 2010 for a discussion of the selection of lens candidates in H-ATLAS and other *Herschel* surveys). This source was therefore observed spectroscopically in the submm. A CO spectroscopic redshift of 3.26 was first suggested by Z-spec (Bradford et al. 2004) observations, then subsequently confirmed by observations by the CARMA interferometer (Leeuw et al., in preparation) and the Zpectrometer instrument (Harris et al. 2007) on the Greenbank Telescope (Harris et al. 2012; see also Fu et al. 2012). Additional followup observations in the optical, near-IR, submm and other wavelengths were targeted at the lensed $z = 3.26$ source and the foreground objects responsible for the lensing, resulting in detailed analyses of this lensing system by Fu et al. (2012) and Bussmann et al. (2013). Their conclusions are that the $z = 3.26$ source HATLAS12-00 is subject to gravitational lensing, with a magnification of 9.6 ± 0.5 in both the submm continuum and CO, and 16.7 ± 0.8 in the K' band, by two foreground galaxies, one at a spectroscopically determined redshift of 1.22, and another with photometry suggesting that it lies at a similar redshift. The submm photometry of HATLAS12-00 at 890 μm acquired with the Submillimeter Array (SMA) as part of this programme (Fu et al.

Table 1. Sources detected with S/N > 4 by the LABOCA observations, giving the position, LABOCA flux and S/N at 870 μm as well as the angular distance from the lensed source HATLAS12-00. LABOCA_1 can readily be identified with the lensed source itself.

Name	RA Deg J2000	Dec. Deg J2000	F870 mJy	S/N	Comments
LABOCA_1	176.658858	-0.191142	79.4 ± 2.5	32.1	5 arcsec from HATLAS12-00, lensed source
LABOCA_2	176.674044	-0.226574	14.8 ± 1.9	7.9	136 arcsec from lens; 5 arcsec from HATLASJ14641.4-001332
LABOCA_3	176.679105	-0.137993	10.3 ± 1.6	6.6	207 arcsec from lens
LABOCA_4	176.598117	-0.183549	10.8 ± 2.1	5.1	220 arcsec from lens; 2 arcsec from HATLASJ14623.5-001058
LABOCA_5	176.684167	-0.145586	7.3 ± 1.5	4.9	190 arcsec from lens; 6 arcsec from HATLASJ14644.6-000840
LABOCA_6	176.608240	-0.155709	8.6 ± 2.1	4.2	223 arcsec from lens
LABOCA_7	176.742378	-0.196203	9.4 ± 2.3	4.0	301 arcsec from lens

2012; Bussmann et al. 2013) is fully consistent with the 870 μm and 850 μm fluxes derived for this source from the LABOCA and SCUBA2 data to be presented here. The spectral energy distribution (SED) of the lensed source, after correcting for the lensing amplification, is well matched by the optically thick SED model for Arp220 from Rangwala et al. (2011), with a lensing-corrected far-IR luminosity of $1.2 \pm 0.2 \times 10^{13} L_{\odot}$, and an implied star formation rate of $1400 \pm 300 M_{\odot} \text{yr}^{-1}$. In many ways the unlensed properties of this object match those of the broader population of bright submm selected galaxies first discovered by the SCUBA submm imager (see e.g. Chapman et al. 2005; Clements et al. 2008; Michałowski, Hjorth & Watson 2010). The unlensed 870 μm flux of this object would be ~ 7.7 mJy.

3 OBSERVATIONS OF THE HATLAS12-00 FIELD

3.1 LABOCA observations

We observed a field of diameter ~ 600 arcsec around the position of the lensed source HATLAS12-00 with the LABOCA 870 μm imager on the APEX telescope (the Atacama Pathfinder EXperiment; Güsten et al. 2006), during ESO programme 088.A-0929. APEX is a 12m diameter submm telescope situated in the Atacama desert, Chile. LABOCA is a multichannel continuum bolometer array mounted on APEX (Siringo et al. 2009) used for continuum imaging at a central wavelength of 870 μm . It has 295 bolometer detectors arranged in concentric hexagons giving a total instantaneous field of view of 11.4 arcmin. The angular resolution is 18.6 arcsec (FWHM) and the channels are separated by 36 arcsec meaning that the field of view is undersampled by the array. We therefore adopted a standard spiral scanning pattern to produce a fully sampled map of the instrumental field of view.

Observations were carried out over five nights from 2011 November 21 to 2011 November 25. The target field was observed for a total integration time of 20 h, in continuous scans of 7 min each. Atmospheric opacities for our observations ranged from 0.158 to 0.357, with a median $\tau = 0.209$. Standard calibrators were observed during the observing run, in-between scientific scans, and included the planets Mars and Uranus, and the stars CW Leonis, B13134 and N2071IR. The radio source J1058+016 was used as a pointing calibrator throughout the whole observing run.

Data reduction used the official data reduction package BOA.¹ This provides a dedicated pipeline for the processing of LABOCA data

and includes automated flux calibration, flatfielding, opacity correction, noise removal, and despiking of the bolometer timestreams. In addition, BOA provides a number of scripts for different reduction schemes, with preset parameters that can be modified by the user. We ran BOA using a modified version of the default script *reduce-map-weaksource.boa*, where we modify the low-frequency filter window to allow less aggressive filtering: this proved necessary because of the presence of the bright lensed source HATLAS12-00 at the centre of the observed field, which generated significant negative lobes if too narrow a filter was used. We found iteratively that a filtering window from 0.25 to 0.4 (compared to the default 0.3–0.35 interval) provided a satisfactory result while efficiently filtering the low-frequency noise. These values are instrumental parameters related to the details of the data reduction software, and are discussed further in section 3.8.4 of the BOA manual (Schuller et al. 2010). The scans are then variance-weighted and co-added to provide final maps of flux density and noise. The final reduced map provides a useful field of $\sim 11 \times 9$ arcmin in size with typical 1σ noise ranging from 1.4 mJy to 2.5 mJy.

Individual sources are extracted from the map using a source-finding algorithm which identifies peaks in a smoothed signal-to-noise map, produced by convolving the flux density map, weighted by the inverse of the variance, with the 18.6 arcsec full width half-maximum (FWHM) beam. Peaks with a signal-to-noise ratio of at least 2.5 were selected as candidate sources, their flux (error) was then calculated as the value of the beam-convolved flux density (noise) map at the position of the peak. We detect seven peaks above a 4σ threshold, four of which have S/N > 5 (see Table 1). One of these, as expected, is the lensed source HATLAS12-00.

3.2 SCUBA2 observations

A field of diameter ~ 700 arcsec around the position of HATLAS12-00 was observed with the SCUBA2 850 & 450 μm imager (Holland et al. 2013) on the James Clerk Maxwell Telescope (JCMT) on Mauna Kea as part of a programme to observe candidate clusters of dusty galaxies detected through cross matching *Planck* and *Herschel* sources. SCUBA2 provides an angular resolution of 14.5 arcsec (FWHM) at 850 μm .

Observations for the programme were carried out over a five night period from 2013 April 8 to 2013 April 12, but the observations of HATLAS12-00 discussed here were taken only on April 8 and 11. Since the target for these observations was the immediate region around the lensed source, we used the DAISY observing mode, which scans the detector arrays in a ‘spirograph’ pattern around the targeted position (in this case HATLAS12-00). This optimises the sensitivity in the central regions of the field, but provides reasonable sensitivity over a larger field. HATLAS12-00 was observed for four

¹ Bolometer Array Analysis Software: http://www3.mpifr-bonn.mpg.de/div/submmtech/software/boa/boa_main.html

Table 2. Sources detected with $S/N > 4$ by the SCUBA2 observations, giving the position, SCUBA2 flux and S/N at $850\ \mu\text{m}$ as well as the angular distance from the lensed source HATLAS12-00 and from any nearby LABOCA sources. As with LABOCA_1, SCUBA2_10 can readily be identified with the lensed source itself.

Name	RA Deg J2000	Dec. Deg J2000	F850 mJy	S/N	Comments
SCUBA2_1	176.6068780	-0.2351671	10.6 ± 2.1	5.0	Out of LABOCA field; 243 arcsec from lens; 4 arcsec from HATLAS_78812
SCUBA2_2	176.6161110	-0.1266438	9.6 ± 2.3	4.2	281 arcsec from lens
SCUBA2_3	176.6811353	-0.1372072	10.5 ± 2.2	4.7	7.8 arcsec from LABOCA_3; 213 arcsec from lens
SCUBA2_4	176.6749951	-0.1491695	8.6 ± 2.0	4.2	165 arcsec from lens
SCUBA2_5	176.6860210	-0.1568639	10.5 ± 2.0	5.3	160 arcsec from lens
SCUBA2_6	176.5883331	-0.1638748	9.9 ± 2.5	4.0	273 arcsec from lens
SCUBA2_7	176.6155570	-0.1716642	8.0 ± 2.0	4.1	172 arcsec from lens
SCUBA2_8	176.6477698	-0.1805539	7.0 ± 1.4	5.0	57 arcsec from lens; 4 arcsec from HATLASJ114635.1-001048
SCUBA2_9	176.6173862	-0.1857557	10.6 ± 1.8	6.0	151 arcsec from lens; 8 arcsec from HATLASJ114628.6-001114
SCUBA2_10	176.6587577	-0.1919366	80.0 ± 1.3	59.7	2.9 arcsec from LABOCA_1; 0 arcsec from lens, lensed source
SCUBA2_11	176.6524809	-0.2122232	6.4 ± 1.5	4.4	76 arcsec from lens
SCUBA2_12	176.6415322	-0.2196134	7.5 ± 1.6	4.7	117 arcsec from lens
SCUBA2_13	176.6738450	-0.2257691	10.0 ± 1.7	5.8	3.0 arcsec from LABOCA_2; 133 arcsec from lens
SCUBA2_14	176.6661112	-0.2338934	7.3 ± 1.8	4.0	153 arcsec from lens

separate observing blocks, each of 30 min duration, for a total integration time of two hours. Three of these blocks were observed on April 8, and one on April 11. Observing conditions were good (grade 2 or upper grade 3, corresponding to 1–2mm of precipitable water vapour) for all of these observations. Standard observatory calibration observations were taken on both nights.

Data reduction used the standard `SMURF` package (Chapin et al. 2013) following the procedures outlined in the SCUBA2 Data Reduction Cookbook (Thomas 2012). The separate scans were reduced using the dynamic iterative mapmaker `makemap`. These were then combined using a noise-weighted optimal method using the `MOSAIC_JCMT_IMAGES` recipe in the `PICARD` environment. Since we are interested in unresolved, faint point sources, we used the `SCUBA2_MATCHED_FILTER` recipe, which removed large angular scale variations in this final map by calculating a smoothed map with a 30 arcsec kernel, subtracting this, and then convolving the map with the $850\ \mu\text{m}$ beam. The resulting image then had the higher-noise edge regions cropped, limiting it to a circular field with diameter 700 arcsec. Calibration from observed detector power to detected flux densities used the standard observatory determined flux calibration factor of $537\ \text{Jy/pW/beam}$ at $850\ \mu\text{m}$. Noise in our final image ranged from $1\sigma = 1.3\ \text{mJy}$ in the centre to $1\sigma = 2.7\ \text{mJy}$ at the edges.

Individual sources were extracted from the map by identifying peaks in the S/N map calculated by dividing the final beam convolved map by the noise map. Applying a 4σ threshold for detection, we find a total of 14 $850\ \mu\text{m}$ sources. Six of these, including the lensed source, have an $S/N > 5$ (see Table 2).

Observing conditions were not good enough for the $450\ \mu\text{m}$ data simultaneously taken with the $850\ \mu\text{m}$ observations to be useful.

3.3 *Spitzer* observations

Spitzer-IRAC 3.6 and $4.5\ \mu\text{m}$ staring mode observations of the extended region covering the clump of sub-mm galaxies around HATLAS12-00 were carried out during the warm mission. In staring mode, simultaneous observations at 3.6 and $4.5\ \mu\text{m}$ are offset from each other by 6.8 arcmin. Due to the offset, $\sim 0.05\ \text{deg}^2$ of the targeted area has imaging data at both 3.6 and $4.5\ \mu\text{m}$, and the remainder split between 3.6 and $4.5\ \mu\text{m}$ coverage. The total exposure time is 1600 s per pixel in each filter with the four-point dithered

map taking over four hours to complete. Data reduction and mosaicking was performed on the Corrected Basic Calibrated Data (cBCD) provided by the *Spitzer* Science Center using `MOPEX` (Mosaicker and Point source EXtractor; Makovoz & Marleau 2005). The final mosaicked images have 0.6×0.6 arcsec pixels and the FWHM of the IRAC point spread function (PSF) at 3.6 and $4.5\ \mu\text{m}$ is 1.66 and 1.72 arcsec, respectively. Source detection is performed with `SEXTRACTOR` (Bertin & Arnouts 1996) and detected sources are required to comprise at least three contiguous pixels with fluxes at least 1.5σ above the local background. Photometry was measured in 3.8 arcsec diameter apertures with the `APPHOT` task in `IRAF`. The advantage of `APPHOT` is that the photometry is measured in fixed apertures at specified source positions. The measured aperture photometry was corrected to total fluxes, assuming point-source profiles, and using the calibration derived by the SWIRE team for IRAC data with multiplicative correction factors of 1.36 and 1.40 at 3.6 and $4.5\ \mu\text{m}$, respectively (Surace et al. 2005).

3.4 Submillimeter array observations

Four regions around HATLAS12-00 were observed in track sharing mode at the Submillimeter Array on Mauna Kea in Compact configuration on 2013 April 7 UTC and 2013 May 16 UTC. The SIS receivers were tuned to an LO frequency of 270.0 GHz. Both observations were made in good conditions, with $\tau_{225} \sim 0.07$ and 10–25 per cent humidity. An additional track in SubCompact configuration was obtained on 2013 May 13 UTC in slightly worse conditions ($\tau_{225} \sim 0.07$ and only 6 antennas) but was combined with the other two tracks for a slight improvement in SNR and a final beam of about 2.7×2.3 arcsec. The targets for these observations were sources LABOCA_2, LABOCA_3, LABOCA_4 and LABOCA_5, with predicted 270GHz fluxes of 8, 4, 6 and 4 mJy, respectively.

The SMA data were calibrated using the `MIR` software package developed at Caltech and modified for the SMA. Gain calibration was performed using the nearby quasars 3c279 and 3c273. Absolute flux calibration was performed using real time measurements of the system temperatures with observations of Titan to set the scale, and bandpass calibration was done using 3c279 and 3c84.

The data were imaged using `MIRIAD` (Sault, Teuben & Wright 1995), and further analysis carried out using the `KARMA` software package. The noise in the final co-added maps ranged from

1–1.3 mJy. A secure source, $>4\sigma$, was only detected in the map of LABOCA_2 with a flux of 4.2 ± 1 mJy. It is also detected in both the individual (uncombined) Compact and SubCompact maps. The brightest sources in the SMA maps associated with the positions of the other LABOCA sources were 3.8 ± 1.3 , 4.3 ± 1.3 and 3.1 ± 1.1 mJy for LABOCA_3, LABOCA_4 and LABOCA_5, respectively, which are compatible with the fluxes predicted for the sources.

3.5 Optical and near-infrared observations

Near-IR observations in the J and K' bands were taken of a $\sim 150 \times 150$ arcsec region around the position of the SMA-identified source LABOCA_2 (see above) using the ISAAC instrument on the VLT. J and K' observations were taken on the 2013 April 19 and 2013 March 12, respectively. Observing conditions for both these observations were good with seeing measured at 0.7 and 0.6 arcsec, respectively. Total on-source integration times were 3240s at J and 1536s at K' . These observations were conducted in service mode. The data were reduced using the standard ESO processing pipeline, and the images were astrometrically and photometrically calibrated using cross identifications with 2MASS sources.

Optical observations using the ACAM imager on the *William Herschel Telescope* were used to provide a deep, white light (ie. filter free) image of the field around the HATLAS12-00 lens. These observations are discussed in detail in Fu et al. (2012) and reach a 5σ detection limit comparable to $i_{AB} = 24.6$.

4 OBSERVATIONAL RESULTS

The SCUBA2 850 μm image is shown in Fig. 1, with the LABOCA S/N contours overlaid. In Fig. 2 we present a three colour SPIRE image of this field (blue for 250 μm , green for 350 μm and red for 500 μm) with the positions of the SCUBA2 and LABOCA detected sources indicated. The lensed source is clearly detected, and a total of 17 other LABOCA and/or SCUBA2 sources are also found with $S/N > 4\sigma$.

4.1 Cross identification with spire sources

To obtain cross identifications and SPIRE flux measurements for the sources found by LABOCA and SCUBA2 we examine both the SPIRE catalogues produced by the H-ATLAS team and the SPIRE maps themselves. We first compare the 850/870 μm sources identified by SCUBA2 and LABOCA to the officially released H-ATLAS source catalogue (Valiante et al., in preparation). This catalogue includes sources detected at $>5\sigma$ significance in at least one SPIRE band. This comparison yields six clear identifications, including the lensed source, with separations between the SPIRE and submm sources of 9 arcsec or less (see Table 3), consistent with the expected combined positional uncertainties of these data sets of ~ 10 arcsec. The fluxes and H-ATLAS names for these sources are reported in Tables 1, 2 and 3 as appropriate. Given the density of 850 μm sources on the sky and our matching radius we expect only ~ 0.07 false positive identifications of a SPIRE source with a submm source over the entire catalogue of 18 submm sources. If we instead use the enhanced submm source density over the field that we find in this region (see Section 4.3) then the number of false positives predicted rises to 0.3. We can thus consider these identifications reliable.

We also compare the LABOCA and SCUBA2 source lists to a supplementary H-ATLAS catalogue generated using the same

MADX algorithm (Maddox et al. 2010; Maddox et al., in preparation) as the main catalogue but extending down to 3σ significance detections rather than the 5σ used for the main catalogue. Cross matching with this extended catalogue provides a further six SPIRE identifications for our LABOCA and/or SCUBA2 sources with separations of 9 arcsec or less. Identifications with this supplementary catalogue are indicated in Tables 1, 2 and 3 as appropriate. One further plausible cross identification, with a separation of 10.8 arcsec is also found, for SCUBA2_2. For these supplementary identifications and for submm sources not directly associated with a catalogued SPIRE source, we estimate their SPIRE fluxes by extracting the fluxes at the LABOCA or SCUBA2 positions from the background-subtracted match-filtered SPIRE maps provided by H-ATLAS. Source fluxes from SPIRE, LABOCA and/or SCUBA2 are shown in Table 3.

One source, SCUBA2_3 (which is cross identified with LABOCA_3 and an H-ATLAS supplementary source) lies fairly close to a second SPIRE source (LABOCA_5) with a separation of ~ 17 arcsec. This is comparable to the size of the SPIRE 250 μm beam and smaller than the 350 or 500 μm beams. The immediate neighbourhood of this source also encompasses the sources SCUBA2_5 and SCUBA2_4, all within an area of about 1 arcmin². The source density in this region is thus substantially higher than the usual one source per 20 beams criterion for confusion (Hewish 1961). We might thus expect problems with flux estimation in this region. To address this issue we extract far-IR fluxes from the H-ATLAS maps at 250, 350 and 500 μm for this confused region using the positions of the submm detected objects, as noted above, as priors. We also perform a simultaneous fit to the maps using four gaussians, with FWHMs corresponding to the instrumental beams at the appropriate wavelength, and with positions corresponding to those of the submm detected objects, to a section of the images around these sources using the image fitting tool `IMFIT` (Erwin 2015).² The gaussians are fitted simultaneously to, in effect, deblend the sources. We found that this deblending procedure produces fluxes which are consistent with those extracted directly from the maps. The deblended fluxes are those given in Table 3.

4.2 Comparison of LABOCA and SCUBA2 source lists

A combination of both the LABOCA and SCUBA2 source catalogues provides a list of 18 distinct sources, with three sources, including the lens HATLAS12-00, appearing in both, and a total of 12 sources cross identified between one (or both) of the submm source lists and the H-ATLAS SPIRE catalogue. This raises the question of the reality of those submm sources detected by one set of observations and not the other. This issue is complicated by the fact that the noise in the two submm data sets is not uniform, by confusion, by different beamsizes, and by the differences in the data reduction methods used by the two bolometer array instruments. To address this further, we have extracted the SPIRE fluxes of each of the submm sources as described above. Where sources are not explicitly detected by both submm instruments, the submm fluxes from the complementary submm map are also extracted. These are given in Table 3.

We assess the reliability of our submm detected sources by comparing the S/N with which they are detected in the five bands

² <http://www.mpe.mpg.de/~erwin/code/imfit/>

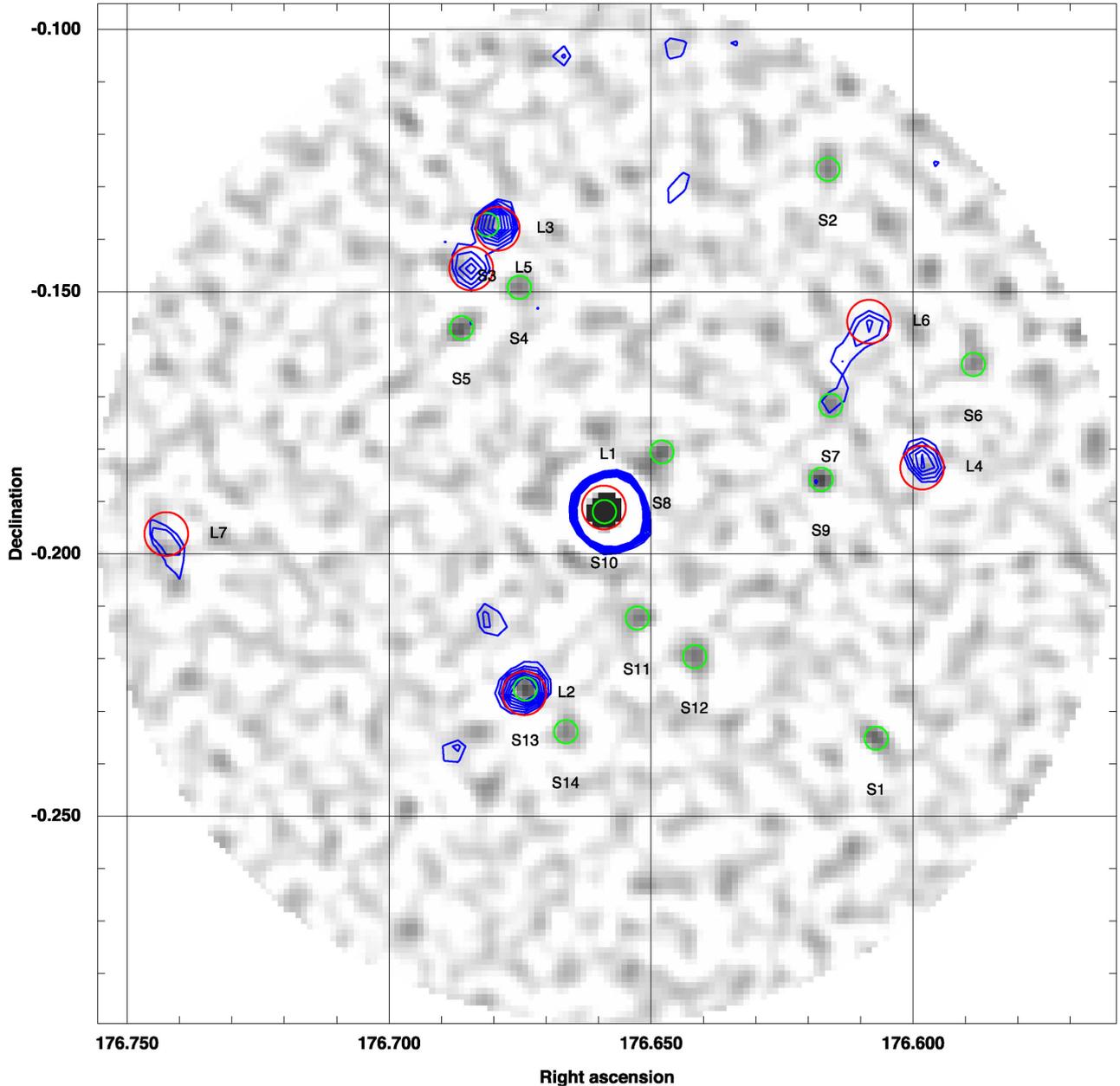


Figure 1. SCUBA2 850 μm image of the clump, LABOCA signal-to-noise contours overplotted in blue, positions of $>4\sigma$ LABOCA sources (red) and SCUBA2 sources (green) indicated by circles. LABOCA S/N contours start at 3σ and rise to 10σ in steps of 1σ . Source position circle size is matched to the beam FWHM of the appropriate instrument. Source names shown in black as L1, S1 etc.. For SCUBA2 sources the name lies below the relevant source, for LABOCA, with the exception of the lensed source, they lie to the right. For the lensed source it lies above. Coordinates are given in degrees J2000.

observed by the three instruments. Sources detected by SCUBA2 and/or LABOCA are considered good if they are detected in a total of at least three bands from SPIRE (250, 350 and 500 μm), LABOCA and SCUBA2. In this context, detection in a SPIRE band is considered to be an $S/N > 3$, whether this comes from the H-ATLAS catalogue or is measured from the H-ATLAS maps. Marginal sources are those detected by only one complementary band, and unreliable sources are those not detected in any complementary passbands. On this basis we have 10 good detections, including the lensed source, 5 marginal detections, and 3 unreliable detections.

As can be seen from the table notes, three of the SCUBA2 sources are found in parts of the LABOCA map where there are problems

with the data reduction. One of these, SCUBA2_8, is close to the bright lensed source HATLAS12-00, and is affected by negative ringing in the LABOCA map production process. Nevertheless, it is clearly detected by SPIRE, so its reality is not in doubt. Two other SCUBA2 sources lie in a region where there is a large-scale gradient in the LABOCA map. We attempt to remove the effects of this gradient by smoothing the LABOCA map with a Gaussian with a 1σ of 1 arcmin, subtracting this from the LABOCA map, and then searching for flux at the positions of these sources. In neither case does this suggest the presence of a source detected by LABOCA at $>3\sigma$, but the presence of this gradient suggests that the LABOCA data in this area may be of a lower quality than the Gaussian noise suggests. The lack of LABOCA confirmation for SCUBA2_12, a

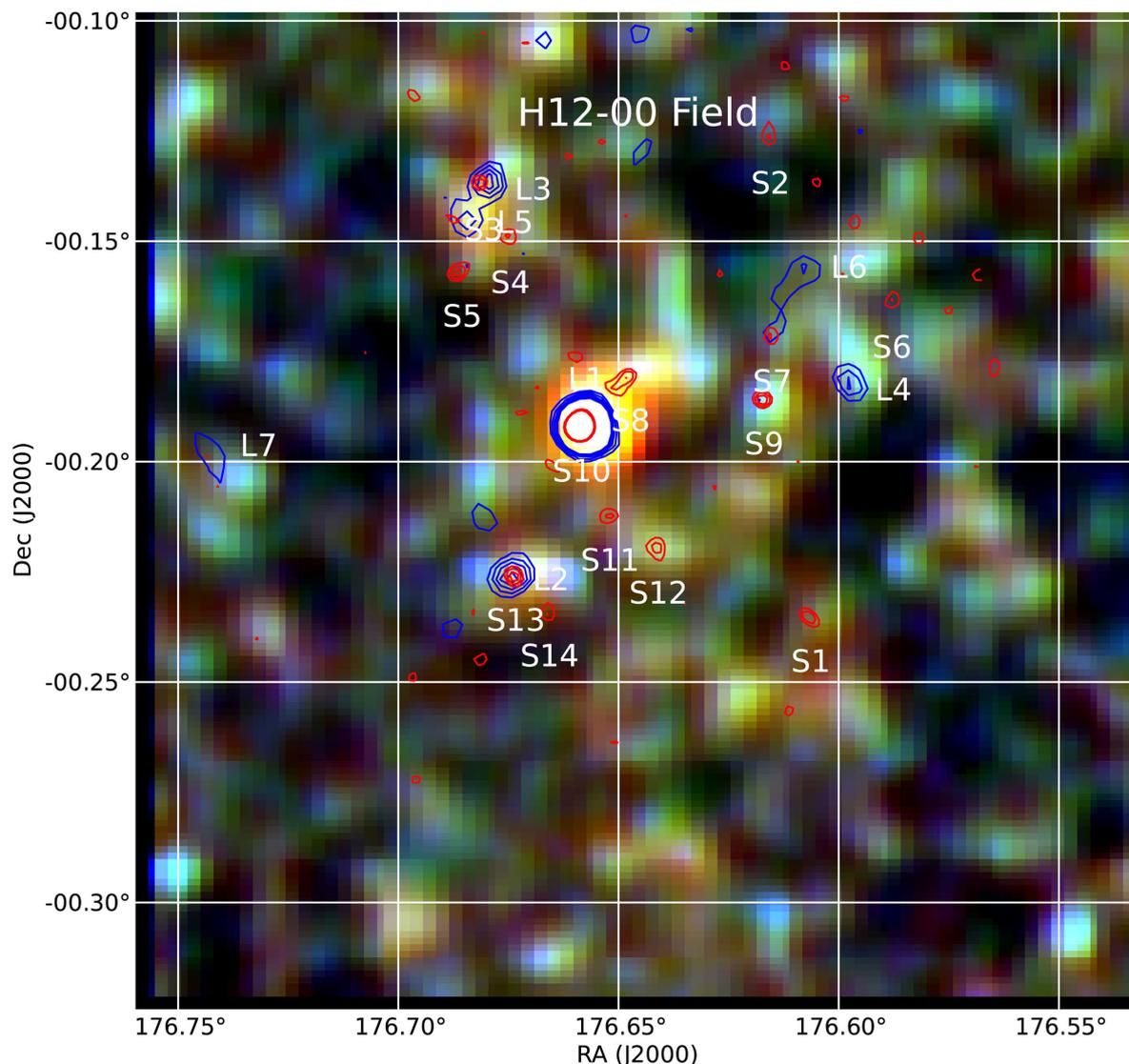


Figure 2. Three colour SPIRE image of the 400×400 arcsec region around the lensed $z = 3.26$ source HATLAS12-00. Blue = $250 \mu\text{m}$, green = $350 \mu\text{m}$ and red = $500 \mu\text{m}$, overlaid by contours, at levels of 3σ , 4σ , 5σ , 6σ and 7σ from the submm observations, with LABOCA in blue and SCUBA2 in red. Source names added as in Fig. 1. Note that those sources brightest at 870 or $850 \mu\text{m}$ are associated with the reddest SPIRE sources.

source clearly detected by SPIRE at $>3\sigma$ in all three bands is thus unlikely to be a problem.

4.3 Source overdensities around HATLAS12-00

Our observations of the region around HATLAS12-00 have uncovered a number of potentially associated sources at both submm wavelengths, as found by SCUBA2 and LABOCA, and in the *Herschel* data themselves. These results are not dissimilar to the submm source overdensities uncovered by Stevens et al. (2010) around quasars, the *Herschel* source overdensities found by Rigby et al. (2014) around some high redshift radio galaxies, the overdensity of *Herschel* and LABOCA sources associated with the Spiderweb galaxy (Dannerbauer et al. 2014), or the *Herschel* and SCUBA2 overdensity found behind the RCS 231953+00 supercluster by Noble et al. (2013). We here quantitatively assess the source overdensities of both submm and *Herschel* sources around HATLAS12-00.

The analysis here, of both SPIRE and submm source densities, compares the source densities associated with our sources to the

density of individual field sources at all redshifts down to the relevant flux limits. The possibility that our clumps might be the result of line-of-sight alignments of several weak, physically unassociated, overdensities, as has been seen, for example, in the optical for Abell clusters (Sutherland & Efstathiou 1991), is discussed in Section 5.2.

4.3.1 SPIRE source density

To determine the level of SPIRE source overdensity around HATLAS12-00 we compare the SPIRE source density around HATLAS12-00 with that in 10 000 randomly selected positions in the H-ATLAS GAMA12 field, which covers approximately 25 deg^2 (Valiante et al., in preparation). For a SPIRE source to be considered real in this comparison we require a 5σ detection in at least one SPIRE band. The furthest good companion source to HATLAS12-00 lies 220 arcsec away so we initially assess the source density within a 220 arcsec radius region for our 10 000 comparison fields. 14 sources are detected by SPIRE at $>5\sigma$ in the 220 arcsec

Table 3. Comparison of fluxes from LABOCA, SCUBA2 and SPIRE for all submm detected sources with cross identifications in the relevant catalogues noted. The errors quoted for SPIRE fluxes include the confusion noise. Notes: [#]SPIRE fluxes measured from the map. ^{*}SCUBA2 flux not from the exact position of the LABOCA source, but from a plausible 3.4σ SCUBA2 detection ~ 4 arcsec from the position of the SPIRE source. [!]SCUBA2 flux not from the exact position of the LABOCA source, but from a possible 3.0σ SCUBA2 detection ~ 10 arcsec from the LABOCA source. [%]LABOCA flux affected by negative ringing from the bright lensed source. [&]SPIRE fluxes extracted from map by deblending using IMFIT.

Name	F_{250} (mJy)	F_{350} (mJy)	F_{500} (mJy)	F_{LABOCA} (mJy)	F_{SCUBA2} (mJy)	Comments	Status
LABOCA_1	290 ± 6	356 ± 7	295 ± 8	79.4 ± 2.5	80 ± 1.4	HATLAS12-00, also SCUBA2_10	Good
LABOCA_2	51 ± 6	54 ± 7	50 ± 8	14.8 ± 1.9	10 ± 1.7	HATLASJ114641.4-001332, also SCUBA2_13	Good
LABOCA_3 ^{&}	24 ± 6	37 ± 7	38 ± 8	10.3 ± 1.6	10.5 ± 2.2	HATLAS supplementary; SCUBA2_3	Good
LABOCA_4	40 ± 6	42 ± 7	14 ± 8	10.8 ± 2.1	6.4 ± 2.1	HATLASJ114623.5-001058	Good
LABOCA_5 ^{&}	26 ± 6	47 ± 7	46 ± 8	7.3 ± 1.5	7.3 ± 2.2 [*]	HATLASJ114644.6-000840	Good
LABOCA_6 [#]	11 ± 6	16 ± 7	7 ± 8	8.6 ± 2.1	0.6 ± 2.3		Unreliable
LABOCA_7 [#]	10 ± 6	10 ± 7	4 ± 8	9.4 ± 2.3	8.2 ± 2.7 [!]		Marginal
SCUBA2_1 [#]	12 ± 6	18 ± 7	18 ± 8		10.6 ± 2.1	HATLAS supplementary; Outside LABOCA field;	Marginal
SCUBA2_2 [#]	18 ± 6	8 ± 7	-2 ± 8	0 ± 2	9.6 ± 2.3	Possible HATLAS supplementary ID	Marginal
SCUBA2_4 ^{&}	16 ± 6	18 ± 7	26 ± 8	3.3 ± 1.5	8.6 ± 2.0	HATLAS supplementary	Marginal
SCUBA2_5 ^{&}	18 ± 6	23 ± 7	27 ± 8	4.3 ± 1.4	10.5 ± 2.0	HATLAS supplementary	Good
SCUBA2_6 [#]	3 ± 6	5 ± 7	-6 ± 8	0 ± 2.5	9.9 ± 2.5		Unreliable
SCUBA2_7 [#]	21 ± 6	23 ± 7	15 ± 8	7 ± 2.0	8.0 ± 2.0	HATLAS supplementary	Good
SCUBA2_8	55 ± 6	65 ± 7	51 ± 8	-2.5 ± 2.4 [%]	7.0 ± 1.4	HATLASJ114635.1-001048; Poor LABOCA data	Good
SCUBA2_9	56 ± 6	60 ± 7	31 ± 8	6 ± 2	10.6 ± 1.8	HATLASJ114628.6-001114	Good
SCUBA2_11 [#]	5 ± 6	11 ± 7	24 ± 8	0 ± 2.3	6.4 ± 1.5	Gradient affecting LABOCA flux	Marginal
SCUBA2_12 [#]	22 ± 6	30 ± 7	24 ± 8	0 ± 2.2	7.5 ± 1.6	HATLAS supplementary; Gradient affecting LABOCA flux;	Good
SCUBA2_14 [#]	4 ± 6	8 ± 7	14 ± 8	0 ± 1.8	7.3 ± 1.8		Unreliable

around HATLAS12-00. Only 5 of our 10 000 comparison positions have a similar or greater source density. The HATLAS12-00 region can thus be regarded as having a probability of only 5×10^{-4} of arising by chance. We also look at the level of overdensity in this field on a range of scales. We find that within 2, 2.5, 3, 4, 5, and 10 arcmin radii the H12-00 region is overdense at the 3×10^{-3} , $< 10^{-4}$ (ie. no other region in our 10 000 comparison fields has a similar SPIRE source density), 3×10^{-4} , 9×10^{-3} , 1×10^{-2} and 2×10^{-2} levels. This confirms the presence of a significant overdensity of SPIRE sources on scales matching the *Planck* beam (~ 2.5 arcmin radius).

If we restrict our analysis to sources detected at 350 μm rather than those detected in any SPIRE band then regions within 2, 2.5, 3, 4, 5 and 10 arcmin of H12-00 are overdense at the 7×10^{-3} , $< 10^{-4}$ (ie. no other region in our 10 000 comparison fields has a similar 350 μm source density), $< 10^{-4}$, 8×10^{-4} , 3×10^{-4} and 3×10^{-4} levels, suggesting the possible presence of an overdensity on larger scales than the *Planck* beam, up to a radius of ~ 10 arcmin. While this would certainly be a large structure in terms of physical size, amounting to about 10 Mpc in diameter if it lies at the same redshift as HATLAS12-00, it is comparable to the scale of the $z \sim 3$ candidate supercluster identified by Noble et al. (2013), through a combination of SPIRE and SCUBA2 data, and a number of other known protoclusters (Casey 2016). Examination of the progenitors of $z = 0$ massive clusters in the Millennium Simulation (Diener et al. 2015) suggests that they can be as large as 20 Mpc across at $z \sim 3$, consistent with the sizes of these overdensities identified in the far-IR/submm.

4.3.2 Submm source density

At submm wavelengths, 850 and 870 μm , we do not have anything comparable to the large GAMA 12 field observed in the same way

as the region around HATLAS12-00 to use as a direct comparison. We thus apply two alternative approaches to the determination of any overdensity of submm sources associated with HATLAS12-00. The first uses the density of submm sources in the field determined by blank field surveys. The largest of these currently available by far is the SCUBA2 Cosmology Legacy Survey (CLS; Geach et al. 2016) which covers a total area of about 5 deg^2 in a variety of different fields. For sources classified as good we find 9 submm companions to the lens, the maximum separation from which is 220 arcsec. Where possible, we combine the 850 and 870 μm fluxes for these sources to get a combined noise weighted average flux. The faintest combined submm flux for a good source is 6.3 mJy for SCUBA2_5. The fluxes for all the other sources are ≥ 7 mJy. Conservatively, since the sources are not spread uniformly through this area, we use this to define a circular region of radius 220 arcsec within which the observed source density can be compared to the field source density at the same flux limits. The SCUBA2 CLS (Geach et al. 2016) measures counts for their survey to be $130^{+6.7}_{-6.4} \text{ deg}^{-2}$ at 6.5 mJy and $208^{+8.5}_{-8.2} \text{ deg}^{-2}$ at 5.5 mJy. Linear interpolation between these two values gives an estimate for the counts at 6.3 mJy to be $145^{+7}_{-6.8} \text{ deg}^{-2}$. This corresponds to $1.7^{+0.1}_{-0.08}$ sources that would be found in this area at the field density, assuming they are distributed randomly. We find nine sources, so the probability of the observed number of companions arising randomly is then 6×10^{-5} .

Real submm sources are, however, not distributed purely randomly, though the clustering between them in the linear regime is unlikely to be sufficient to substantially reduce the significance of the source overdensity we have found compared to the field (see e.g. Noble et al. 2013). Nevertheless, to be certain that this is not a problem we use a similar method to that used in Section 4.3.1 for SPIRE sources as a second approach to determine the significance of the submm source overdensity. For this we use the SCUBA2

CLS observations of the COSMOS field, covering $\sim 0.65 \text{ deg}^2$, and the UDS field, covering $\sim 1 \text{ deg}^2$, as comparisons since these are the two largest contiguous fields in the survey, and, once again, compare the number of good sources found in regions of a specific size around HATLAS12-00 to 10 000 randomly selected reference positions in the field. We do this for regions within 2, 2.5, 3 and 4 arcmin of H12-00. We find that within 2, 2.5, 3, and 4 arcmin radii the H12-00 region is overdense at the 2.5×10^{-2} , 1.8×10^{-2} , 1.5×10^{-3} , and 6.5×10^{-4} levels. This confirms the presence of a significant overdensity of submm sources. It should be noted that the comparison fields for this analysis are small in size compared to the 25 sq. deg. comparison field used for SPIRE. There is thus a possibility for some cosmic variance effects, but they are unlikely to substantially reduce the significance of this overdensity. These will also be somewhat ameliorated by combining the results, as we have done above, for the UDS and COSMOS fields.

We also compared the density of good sources around HATLAS12-00 to the SCUBA2 source overdensity discovered by Noble et al. (2013), suggested, on the basis of *Herschel* to SCUBA2 colours, to be a protocluster at $z \approx 3$. Both SCUBA2 maps have roughly equal 1σ sensitivities of $\sim 1.5 \text{ mJy}$. Around HATLAS12-00, we detect a total of nine good sources over an area covering approximately 100 arcmin^2 . This corresponds to a source density of ~ 324 sources per deg^2 . This compares to the 16 sources detected by Noble et al. (2013) over approximately 470 arcmin^2 , which gives a surface density of ~ 122 sources per deg^2 . From this, we infer

that HATLAS12-00 is one of the strongest overdensities of $850 \mu\text{m}$ sources currently known, with a surface density $> 2.5\times$ that of the structure detected by Noble et al. (2013).

4.4 *Herschel*-submm colours

The use of SPIRE colour–colour diagrams to constrain redshifts is well established (e.g. Amblard et al. 2010; Negrello et al. 2010; Schulz et al. 2010; Herranz et al. 2013; Noble et al. 2013; Wardlow et al. 2013; Clements et al. 2014) though their interpretation can be uncertain. The observed colours of sources are compared to the colours, as a function of redshift, of the SEDs of known low redshift template objects, such as the starburst galaxy M82 or the nearest ULIRG, Arp220. We have 10 good sources associated with HATLAS12-00, including the lens, for which reasonable quality SPIRE and submm data are available. The SPIRE colours for these sources are shown in Fig. 3, together with the SPIRE colours for the 32 SPIRE-detected sources with $S/N > 2$ in all bands that lie in the submm fields that were not detected at $> 4\sigma$ in the submm. We extend this to the submm in Fig. 4, plotting SPIRE 250-to-350 μm colour against 350-to-850 μm . We have also included the SED of a cold spiral galaxy to illustrate the effects of the dust temperature–redshift degeneracy, whereby a source with colder dust can have similar far-IR-submm colours to those of a higher redshift higher dust temperature object. The dust temperature for this cold galaxy template is $T = 20 \text{ K}$, and the SED is comparable to that of the local spiral M100 (Cortese et al. 2014).

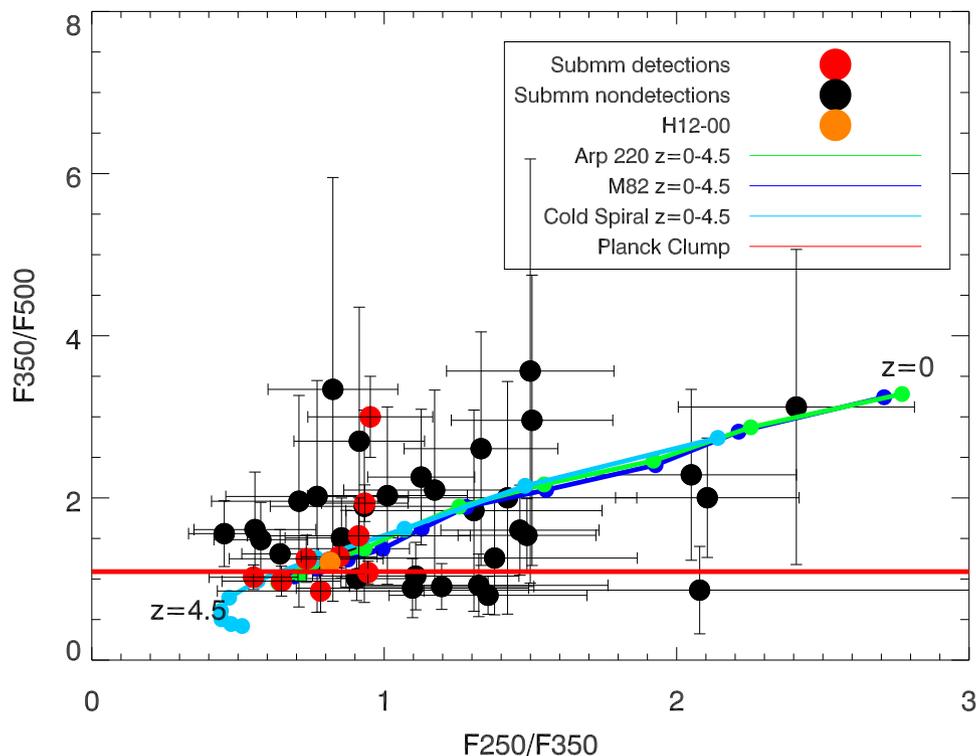


Figure 3. $250 \mu\text{m}/350 \mu\text{m}$ versus $350 \mu\text{m}/500 \mu\text{m}$ flux ratios of SPIRE sources within 5 arcmin of the lensed source HATLAS12-00 compared to those expected for star forming galaxies as a function of redshift. Submm detected sources are indicated with a red colour, with HATLAS12-00 shown in orange. Black symbols denote SPIRE sources that do not have a $> 4\sigma$ submm detection but which have $S/N > 2$ in all SPIRE bands. The submm-detected sources are redder than the bulk of the SPIRE sources, and have colours comparable to those of the lensed $z = 3.26$ source HATLAS12-00. Some SPIRE-only sources have similarly red colours. The *Planck* 857 GHz (ie. $350 \mu\text{m}$) to 545 GHz (ie. $550 \mu\text{m}$) colour is shown as a horizontal red line, giving the colour of the clump as a whole. The *Planck* colour is comparable to that of the lensed source. Colour tracks are also shown as lines for three template SEDs, two (M82 and Arp220) appropriate for starbursting galaxies, one (cold spiral) appropriate for lower temperature lower luminosity systems. These cover the redshift range from $z = 0$ to $z = 4.5$. Dots along these lines occur at intervals of 0.5 in redshift.

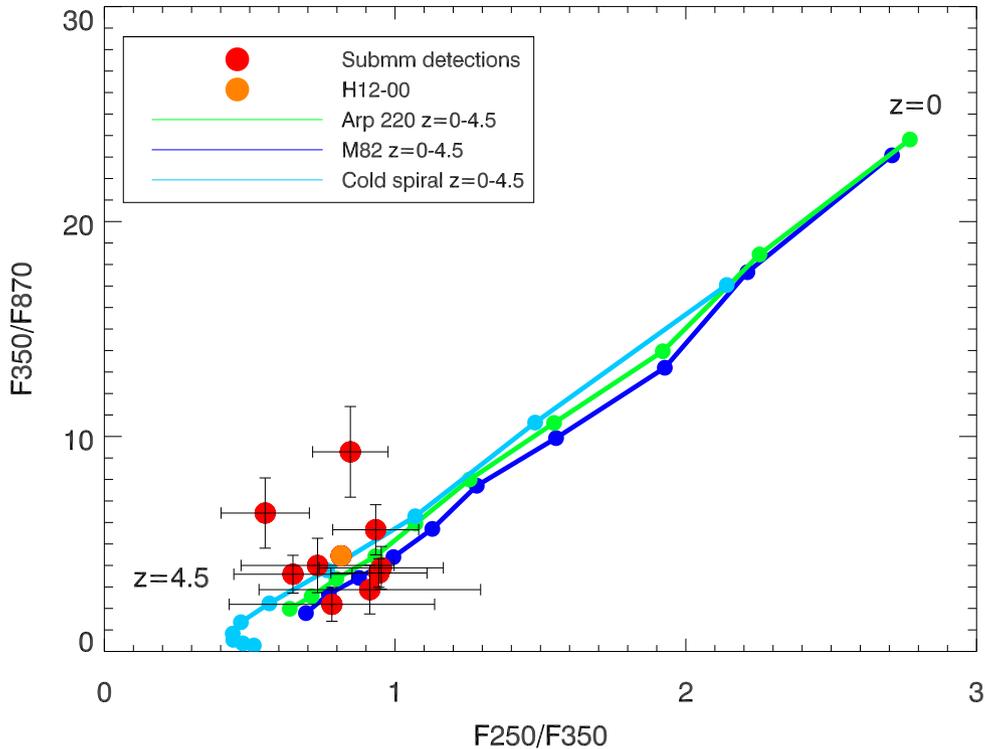


Figure 4. $250\ \mu\text{m}/350\ \mu\text{m}$ versus $350\ \mu\text{m}/870\ \mu\text{m}$ flux ratios of the sources detected in the submm classified as good, compared to colour tracks as a function of redshift for star forming galaxies. All these sources have colours similar to the lensed $z = 3.26$ source HATLAS12-00, which is the source in this figure with the smallest error bars, consistent with them all lying at a similar redshift. Template colour tracks are also shown, similar to those in Fig. 3.

The *Herschel* and *Herschel*-submm colours of our submm detected sources are all quite similar to the colours of the $z = 3.26$ lensed source. There is thus a temptation to conclude that the submm companions of HATLAS 12-00 all lie at a similar redshift. However, there is also the possibility that the clump of sources, while at high redshift, is not physically associated with the lensed source, as well as the possibility that some, or maybe all, of the companions are cooler objects at a significantly lower redshift. If we take the 20 K dust temperature of the cold spiral SED as a likely lower limit to the dust temperature of a galaxy – something that appears to be the case for the vast majority of local galaxies but with a small number of exceptions (Rowan-Robinson & Clements 2015) – then the likely lower redshift limit for these sources is $z > 1$ and for most $z > 1.5$. These limits largely come from the *Herschel*-submm colours.

It is also worth noting that eight of the nine good companions to HATLAS12-00 have $F250/F350 < 1$ ie. their SEDs peak in the $350\ \mu\text{m}$ band of SPIRE. The remaining source has an SED rising to $500\ \mu\text{m}$. Tens of ‘350-peaker’ sources now have spectroscopic redshifts as a result of followup observations aimed at candidate lenses and other samples (e.g. Casey et al. 2012a,b; Harris et al. 2012; Bussmann et al. 2013; Wardlow et al. 2013). The vast majority of those with secure colours and reliable redshifts have redshifts $\gg 2$. Thus, despite the redshift–temperature degeneracy, an SED peaking at $350\ \mu\text{m}$ seems observationally to be a very good indication of high redshift.

4.5 Multiwavelength cross identifications

SMA observations of sources LABOCA_2, 3, 4 and 5 have found a source corresponding to LABOCA_2, with a flux of 4.2 ± 1 mJy (a 4.2σ detection). The location of this SMA source is well matched to the LABOCA and SCUBA2 positions (see Fig. 5). The non-

detections for LABOCA_3, LABOCA_4 and 5 are compatible with their expected fluxes based on their colours and SED template fitting – we would at best only have expected to detect them at $\sim 3\sigma$ given the noise achieved at the SMA, and indeed some marginal detections at this level are found (see Section 3.4).

The position for the SMA counterpart to LABOCA_2 is coincident with a source in our *Spitzer* 3.6 and $4.5\ \mu\text{m}$ images of this field (see Fig. 5 top). The properties of this cross identification are summarized in Table 4. Examination of SDSS images at the position of this source fails to find any optical counterpart, implying that the *i*-band magnitude of the source is fainter than the 21.3 mag *i*-band limit of SDSS. Deeper optical observations of this source obtained with white light (ie. filterless) observations at the *WHT* also fail to find an optical counterpart. The 5σ detection limit for these observations is estimated to be $i_{\text{AB}} < 24.6$ (Fu et al. 2012). This source is detected in our ISAAC J and K’ observations of a $\sim 150 \times 150$ arcsec field around the position of LABOCA_2. J and K’ magnitudes for this source were extracted with apertures matching those of the IRAC photometry, and found to be $J_{\text{vega}} = 22.6 \pm 0.15$ and $K_{\text{vega}} = 20.3 \pm 0.15$. The colours of this source would classify it as a Distant Red Galaxy (DRG; Franx et al. 2003), a class of object already known to often be the near-IR counterparts of high redshift ($z > 2$) submm sources (Dannerbauer et al. 2004).

In Fig. 6 we plot the observed optical/near-IR SED of LABOCA_2, including the IRAC and ISAAC detections and the *WHT* upper limit. We perform a photometric redshift analysis of these fluxes using the template SEDs derived by Berta et al. (2013) for *Herschel* sources and the wider range of optical/near-IR templates provided by Bruzual & Charlot (2003). A variety of templates can fit the data and provide a range of acceptable redshifts from 2.8 to 3.9 for the Berta templates and at $z > 2$ for the Bruzual & Charlot models. None of the templates, however, provides an acceptable

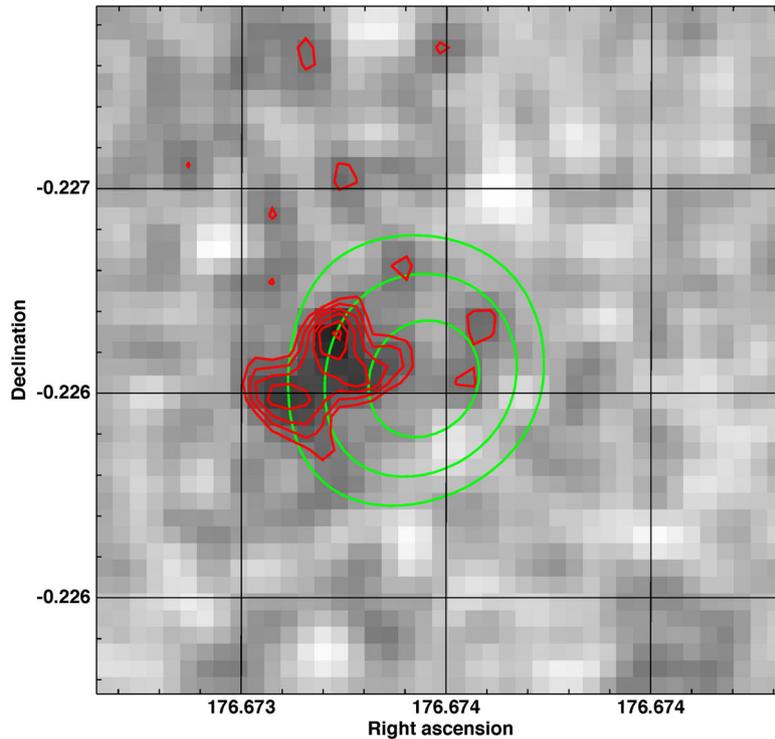
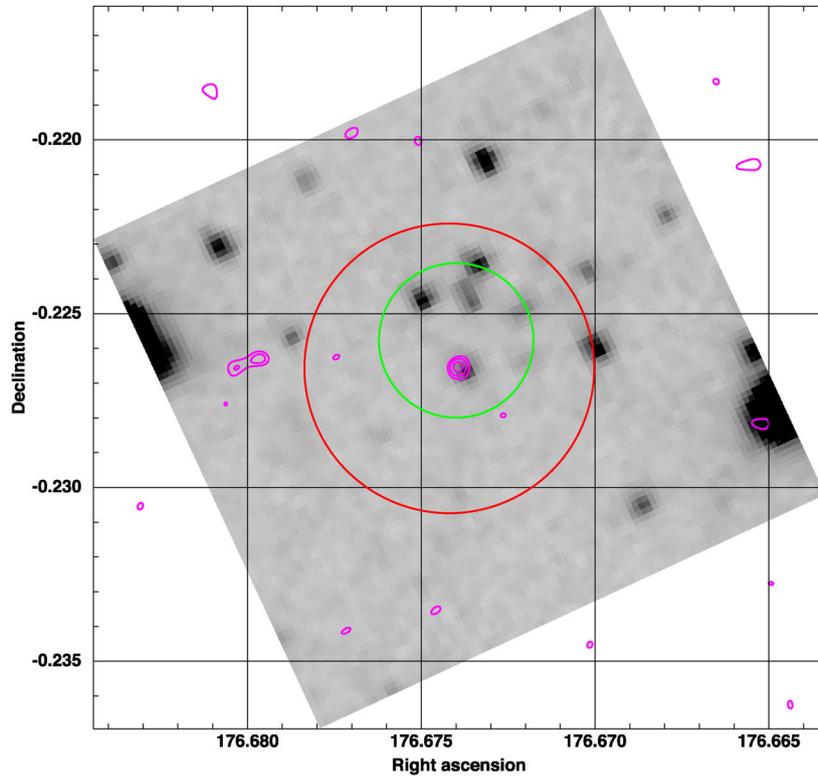
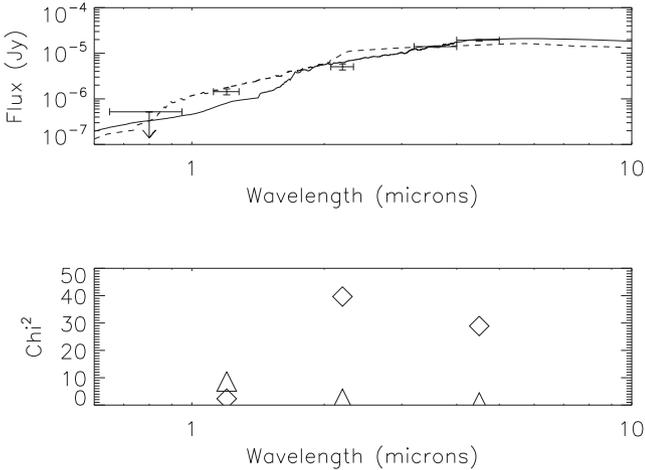


Figure 5. Top: identification of LABOCA_2 with an IRAC source. The grey-scale image is a segment of the larger IRAC 3.6 μm image. The magenta contours are from the SMA, at levels of 2σ , 3σ and 4σ , the red circle is the LABOCA beam at the position of the source, and the green circle is the SCUBA2 beam at the position of the matching source. The correct IRAC identification for this source is clear once the SMA contours are considered. Bottom: SMA contours for the LABOCA_2 source (green) overlaid on a K' band image of the source obtained from ISAAC (grey-scale and red contours). The image is 6×6 arcsec in size with 0.15 arcsec pixels. The original image has been smoothed with a Gaussian of width two pixels to enhance the S/N. Note that the K' band counterpart to the SMA source is extended and seems to have a bimodal morphology, suggestive of a galaxy interaction or merger. For both images coordinates are given in degrees J2000.

Table 4. Data for the source detected by the SMA and cross identified with a *Spitzer* IRAC source. The magnitudes of the source in the IRAC bands are isophotal corrected total magnitudes and given in the Vega system.

Source	RA Deg J2000	Dec. Deg J2000	F_{1100} mJy	Optical AB	J Vega	K' Vega	[3.6] Vega	[4.5] Vega
LABOCA_2	176.6736	-0.2266	4.2 ± 1.1	$i_{AB} > 24.6$	22.6 ± 0.18	20.3 ± 0.15	18.26 ± 0.04	17.42 ± 0.04

**Figure 6.** Top: observed fluxes of LABOCA_2 from IRAC, ISAAC and the *WHT* compared to the best-fitting Berta et al. (2013) template SEDs at $z = 3.26$ (solid) and $z = 1.22$ (dashed), respectively matching the redshift of the lensed source and putative cluster, and the foreground galaxies that are lensing HATLAS12-00. The templates are normalized to the observed flux at $3.6 \mu\text{m}$ from IRAC. Bottom: the χ^2 derived from comparing these fits to the data for the $z = 1.22$ model (diamonds) and the $z = 3.26$ model (triangles). As can be seen the $z = 1.22$ SED is a poorer fit to the data.

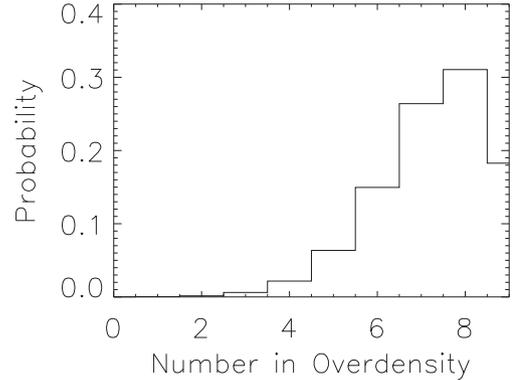
match to the observed SED at redshifts ~ 1 . We thus conclude that the companion source LABOCA_2, at least, is much more likely to lie at a redshift comparable to that of the lensed source than that of the lower redshift lens. In Fig. 6 we illustrate this by comparing the best-fitting Berta template SEDs for $z = 3.26$, matching that of the lensed source and representing a high redshift solution, with that for $z = 1.22$, matching the redshift of the foreground lensing sources and representing a low redshift solution. We also show the χ^2 values for these fits. The high redshift SED is clearly the better fit, with a reduced χ^2 of 3.9 compared to 23.6 for the low redshift solution, though the J band flux is somewhat higher than the template would suggest. Combining the optical/near-IR data with the far-IR/submm fluxes and fitting with the same Berta et al. (2013) templates provides a similar result.

Examination of the ISAAC images shows that LABOCA_2 appears to be extended on scales of a few arcseconds (see Fig. 5 bottom). The source seems to have a bimodal flux distribution, suggestive of a merger-like morphology though other interpretations are possible. However, deeper observations are required to confirm this.

5 DISCUSSION

5.1 The number of sources in the overdensity

We have found a significant overdensity of both SPIRE and SCUBA2 sources in the region around the $z = 3.26$ gravitationally lensed far-IR luminous galaxy HATLAS12-00. While the overdensity is highly significant, the underlying field source counts are

**Figure 7.** The number of sources associated with the overdensity rather than the field versus the probability of this occurring, calculated using equation (1) and the numbers appropriate for good sources within 220 arcsec of HATLAS12-00.

sufficiently high that it is unlikely that all of the sources around HATLAS12-00 are members of the overdensity. The probability that a given number of objects are part of the overdensity, as opposed to being from the field population, can be calculated from the field source counts using Poisson statistics, under the assumption that field sources are distributed at random. The probability that there are n overdensity sources out of M detected sources is thus:

$$p(n|M, \mu) = \frac{\binom{\mu(M-n)}{(M-n)!} e^{-\mu}}{\sum_{i=0}^{i=n} \binom{\mu(M-i)}{(M-i)!} e^{-\mu}} \quad (1)$$

where μ is the number of field sources that would be predicted in the region of consideration on the basis of the source counts.

To illustrate this for the current case we use the CLS field counts from SCUBA2, and restrict ourselves to examining the nine good companion sources which lie within a 220 arcsec distance from HATLAS12-00. The field counts would predict 1.7 sources in such a region. The resulting probabilities for the number of overdensity sources is shown as a histogram in Fig. 7. As can be seen, the predicted number of overdensity sources is fairly uncertain, with the most likely numbers ranging from 6 to 9.

5.2 The nature of the overdensity

The foregoing analysis suggests that a significant fraction of the sources we have detected around HATLAS12-00 are likely to lie in an overdensity of objects. It is a natural step from this result to think that these objects are part of a single coherent physical structure, possibly a cluster or protocluster of galaxies. Similar arguments have been applied to the *Herschel* and submm source overdensities found by others, including Stephens et al. (2010), Noble et al. (2013), Valtchanov et al. (2013), and Dannerbauer et al. (2014). The similarity of the SPIRE and submm colours of these sources lends credence to this suggestion, but we must be careful since there is a long history of apparent overdensities being identified with single structures when they are in fact chance superpositions

of two or more weaker overdensities that just happen to lie along the line of sight (e.g. Sutherland & Efstathiou 1991). We can assess this possibility by looking at the expected number of clusters that would lie in the volume observed in this study. The cluster X-ray luminosity function down to $\sim 1 \times 10^{43} \text{ ergs s}^{-1} \text{ cm}^{-2}$, appropriate for poor clusters or galaxy groups (Koens et al. 2013), is known out to $z \sim 1$ with reasonable accuracy. Since this is expected to decline to higher redshifts it can be used to calculate conservative upper limits to the expected number of clusters found in any $z > 1$ survey. If we were to assume that the HATLAS 12-00 field was selected at random, then the total volume along the line of sight that we have observed out to $z = 3.26$ is $3.8 \times 10^5 \text{ Mpc}^3$ and we would predict an average of ~ 0.38 poor clusters or groups to lie in this volume. Assuming Poisson statistics, one group/cluster would be found with a probability of 0.26, two with 0.05 and three or more structures with 0.007. There is thus a small (~ 6 per cent) but non-negligible chance that our overdensity might be enhanced by a superposition effect.

Obtaining spectroscopic redshifts for the *Herschel* and submm sources we have uncovered is necessary for properly understanding this overdensity. Unfortunately such data is not yet available, but we can get some hints as to what might be going on by applying far-IR photometric redshift techniques, similar to those used by Noble et al. (2013) in studying a submm source overdensity at a suggested redshift of $z \sim 3$ which they uncovered behind the $z = 0.9$ supercluster RCS 231953+00. This process produces a similar result to that found by comparing the colour tracks of template sources to the observed colours of our sources: the higher luminosity, higher dust temperature templates imply redshifts $z \sim 3$, with implied luminosities of $7\text{--}14 \times 10^{12} L_{\odot}$ for the sources we classify as good, while the lower temperature, lower luminosity templates imply redshifts closer to $z \sim 1$ with luminosities $1\text{--}2 \times 10^{12} L_{\odot}$. Noble et al. (2013) argued that lower temperature, lower redshift solutions were not compatible with the empirical temperature-luminosity relation derived by Roseboom et al. (2012) for *Herschel* selected sources. However, further work since then (e.g. Casey et al. 2012b) has shown that there is a significant amount of scatter in this relation. This weakens any conclusion that can be drawn from such an analysis. While higher redshifts for our sources are still somewhat favoured by the $T\text{--}L$ relation in Casey et al. (2012b) the possibility that some of our sources are cool outliers in this relation cannot be discounted. Our analysis of the optical/near-IR SED of the one source where we have a clear identification, LABOCA_2 (see Section 4.5), seems to favour higher redshifts, but without enough precision to differentiate between $z \sim 2$ and $z \sim 3$.

6 CONCLUSIONS

The lensed $z_{\text{spec}} = 3.26$ dusty starburst galaxy HATLAS12-00 was found to be associated with a *Planck* ERCSC source by Herranz et al. (2013), leading to the suggestion that it is part of a galaxy cluster or protocluster, several of whose members are undergoing a starburst. The presence of a number of *Herschel* sources near to HATLAS12-00 with similarly red SPIRE colours to the lens supports this idea. We obtained submm observations of an ~ 11 arcmin diameter field around HATLAS12-00 using both the LABOCA and SCUBA2 submm mappers. As well as detecting the lensed source itself, we detect 17 other submm sources in this field at 4σ significance or greater, with fluxes from 6.4 to 15 mJy at 850 and/or 870 μm . The number of such submm sources found in this field represents a significant overdensity, one that would occur at random in the field with a probability ranging from 7.6×10^{-3} to

3.8×10^{-4} , depending on the reliability of the sources included in the calculation. There is also an overdensity of *Herschel* sources around HATLAS12-00 which has a probability of 5×10^{-4} of arising at random. These low probabilities argue for a physical association between these sources, suggesting that they lie in a cluster, a proto-cluster or some other large scale structure at similar redshifts. Whether this structure is related to the $z = 3.26$ lensed source is unclear. The *Herschel* and submm colours of the sources are red, suggesting that the sources are either warm high luminosity systems at $z > 2$ or cooler systems at a redshift closer to 1. Multiwavelength followup observations identify one of the companions to HATLAS12-00 with a source detected by *Spitzer* at 3.6 and 4.5 μm , and in subsequent near-IR imaging using the VLT. Photometric redshift analysis of the optical/NIR SED of this source indicates a redshift > 2 , potentially similar to that of HATLAS12-00 but not compatible with redshifts ~ 1 . Further followup observations including optical/near-IR imaging and spectroscopy are needed to firmly establish the nature of the overdensity we have found and to examine the tantalising possibility that this might be a galaxy cluster/protocluster at $z \sim 3.26$.

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